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MathCAD

“ ”

2006

519.6
22.19
67

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(1.4/18- -807 19.09.2006)

-19 · „ , · „ · „ MathCAD.
« » : .
: , 2006. – 108 .
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ISBN 966-379-101-2

MathCad.
519.6
22.19
© · „
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· „
· „, 2006
© , 2006

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2	'	79
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9	-
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	107

() , Windows 2000
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 , Windows.
 MathCad , -
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 Math ad.

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Math ad.

1.1

MathCad

MathCad

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Windows.

MathCad

Windows

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(. 1)

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(2).

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(3,

4-).

(. 1):

File / -

(2-1);

Edit / -

(2-2);

View / -

(2-3);

Insert / -

,

(2-4);

Format / -

-

-

(2-5);

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,

:

Calculator Toolbar/

(3-1);

Graph Toolbar /

(3-2);

Vector and Matrix Toolbar /

(3-3);

Evaluation Toolbar/

(3-4);

Calculus Toolbar/

(3-5);

Boolean Toolbar/

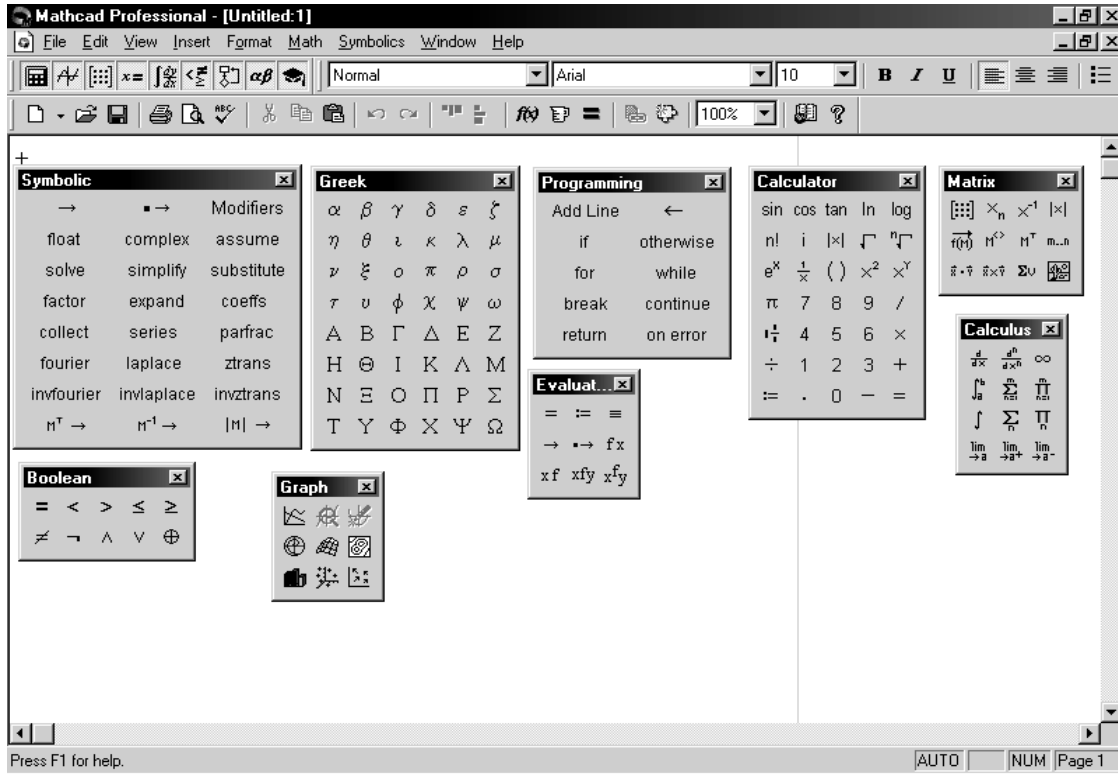
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Programm ng Toolbar/ (3-7);
Greek symbol Toolbar/ (3-8);
Symbol c Keyword Toolbar / (3-9).

New / (4-1);
Open / (4-2);
Save / (4-3);
Pr nt / (4-4);
Pr nt Prev ew / (4-5);
Check Spell ng / (4-6).
Cut / () (4-7);
Copy / () (4-8);
Paste / () (4-9);
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Insert Un t / (4-15);
Calculate / (4-16);
Insert G perl nk / (4-17);
Insert Component / (4-18);
Zoom / (4-19);
Resource Center / (4-20);
Help / (4-21).

MathCad :
Resource Center / -
 (4-20) -
Help / (4-21) -

Sh ft+F1



1 –

MathCad Professional 2001

1.2

$$(M), \quad (X), \quad (X \quad X_j), \quad (X) \quad F(x, y, z).$$

(4-14) f(x) (insert Funct on /).

=,
Math - Automatic Calculation /
 /
F9.
ESC
F9
 - Cut / **Edit - Delete /**
Copy /
) 3-9 (. 1) (-
Enter.
 :=,
Edit - Select All /
 " "
 () -
Math - Options /
 :
 ∞ - 10^{307} ;
 - 2,71828182845905;
 π - π , 3,14159265358979;
 - 1 ;
j - 1j;
 % - 0,01 (, 20 · 30% = 6);
TOL - 0,001;
ORGAN - 1- (), -
 0.

1

= 3 (-

MathCad).

x := 3

$$\sqrt{\frac{4}{e^x}} - \coth(x)^3 \cdot \cos(|x \cdot \sin(x^2) - \ln(x)|) = -0.559$$

1

MathCad.

2

MathCad.

3

/

4

MathCad.

2

2.1

$$y(t) := \sin(t) - \cos(t)$$

t

[-2; 2]

0,5,

:

1

:

t := -2, -1.5 .. 2

-2 -

; -1,5 -

[-2 + 0,5 = -1,5]; ..

Vector and Matrix Toolbar - Range Variable /

/

(); 2 -

2 $y(t) := \sin(t) - \cos(t).$
 3 $t = ($ $t).$
 4 $y(t) = ($ $y(t)).$
 , 1 10 ,
 . 10 -
 10 -
 . -

Math ad:

$t := -2, -1.5 \dots 2$
 $y(t) := \sin(t) - \cos(t)$

t =	y(t) =
-2	-0.493
-1.5	-1.068
-1	-1.382
-0.5	-1.357
0	-1
0.5	-0.398
1	0.301
1.5	0.927
2	1.325

2.2

1 , , :

2 **Format – Result /** - .

(Number of decimal places), -

(Exponential threshold) p.


3 **Exponential threshold /**

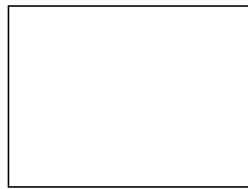
3. , , 102,

. Math ad .

2.3

Math ad

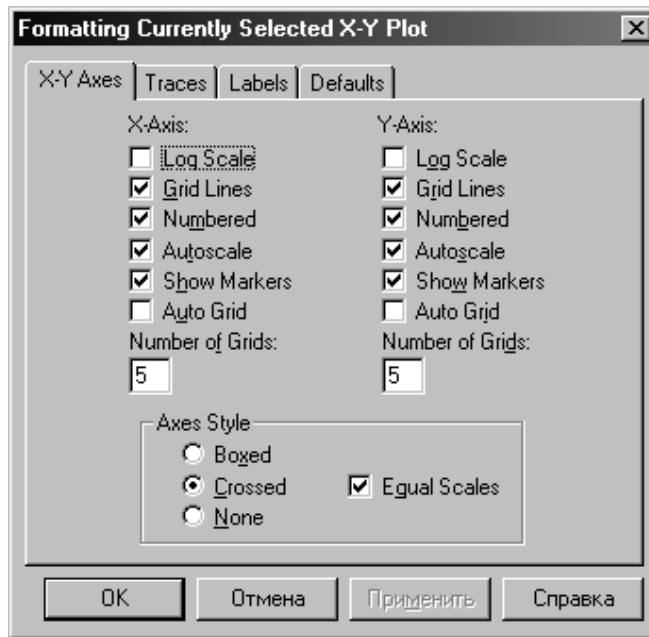
, , ,
.
, ,
: MathCad
.
,
y(t), :
1 () y(t)
Graph Toolbar - X-Y Plot / - X-Y : 
Insert - Graph - X-Y Plot/
X-Y). (. 2).



2 -
2 , t,
3 , t.
, y(t). ,
(
,). , MathCad
4 .
, y (t) ' .
Format - Graph - X-Y Plot /
- X-Y
.
(. 3, 4).

- **Axes** (. 3):

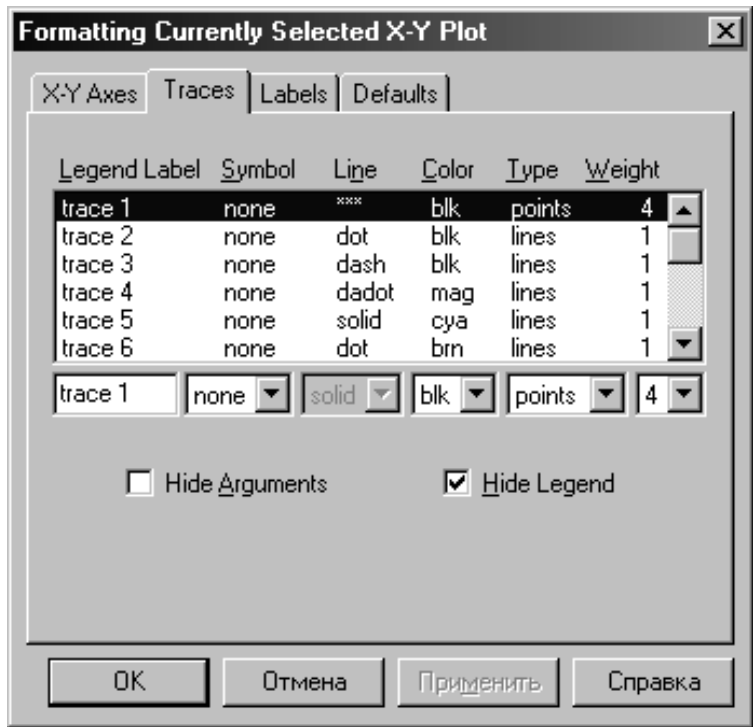
- Log scale** – ;
- Grid lines** – ;
- Numbered** – ;
- Auto scale** – ;
- Show markers** – ;
- Auto grid** – ;
- Number of grids** – ;
- Boxed** – ;
- Crossed** – ;
- None** – ;
- Equal Scales** – .



3 – . - *Axes*

(**Weight**) (Symbol), (Line), (Color),
Traces (Type) ,
 (. 4).

(,) .
 (**F9**).



4 –

Traces

,
(
,
)
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,
()
,
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,
MathCad
()

2

$$y(x) = 3 - \cos(x^2) \quad f(t) = 2 \cdot \sin(2 \cdot t)$$

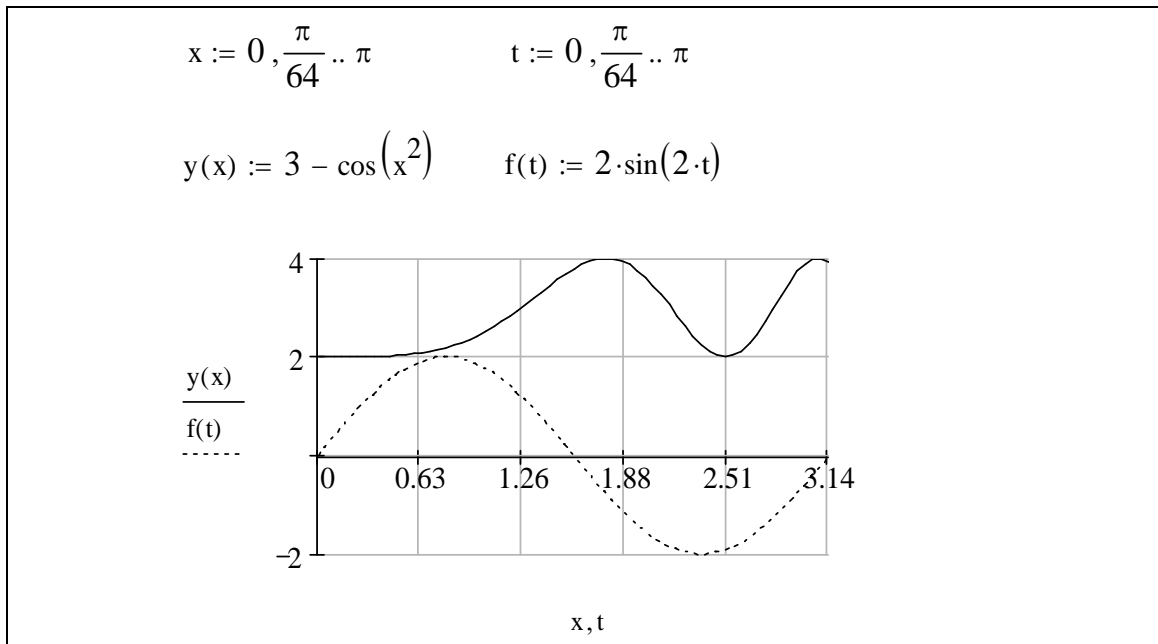
$[0; \pi]$

$\pi/64$.

MathCad

5.

: , " "



5 -

2.4

W -


- **R(w).**

Format - Graph - Polar Plot / - -

(Rad al) (Angular), -

(Per meter).

Insert - Graph - Polar Plot / -

 **Graph Toolbar**

R(w).

:

1

2

MathCad

3 **W** **R(w).**

4 **R - w.**

5 -

R (w).

. MathCad

R(w),**w,**

3

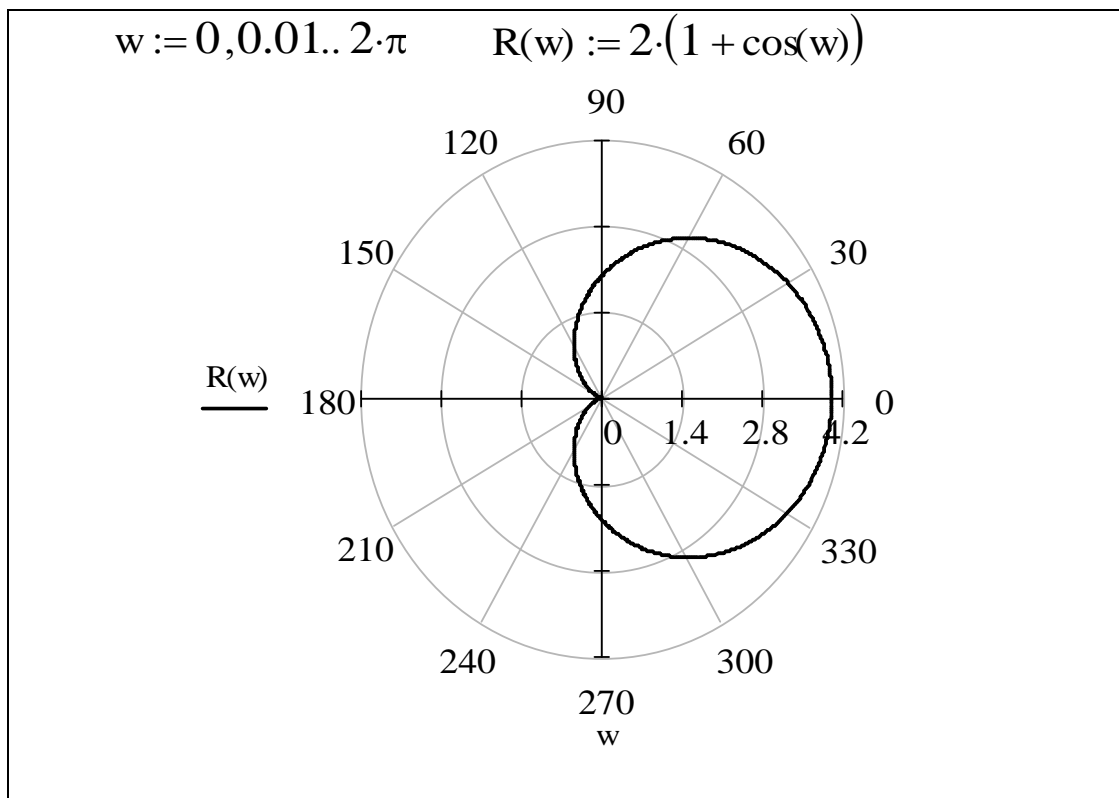
$$R(w) = 2 \cdot (1 + \cos(w))$$

[0; 2]

0,01.

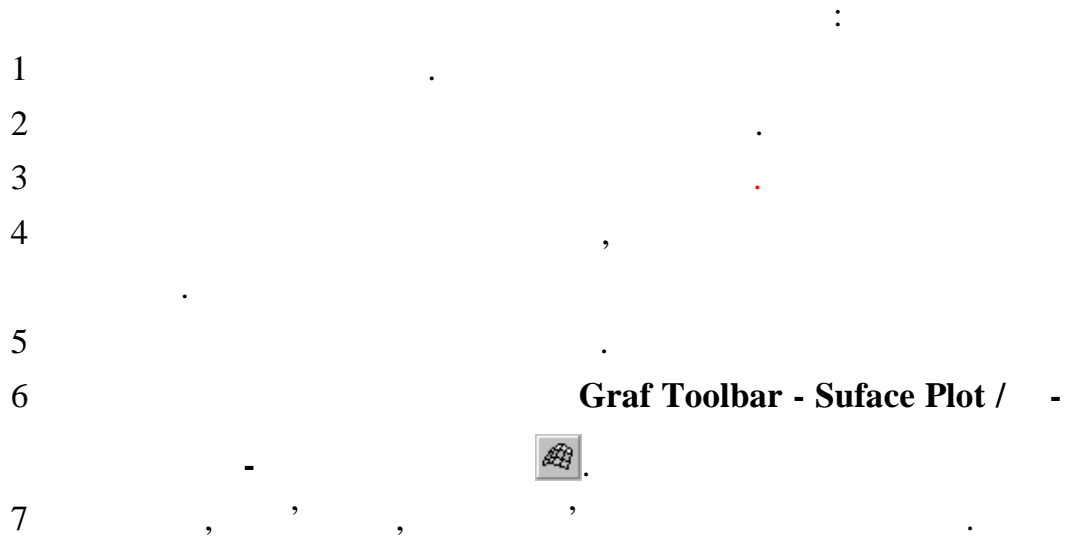
MathCad

6.



6-

2.5



4

$$f(x,y) = \cos(x) + \sin(y) \quad \in [0; 2]$$

$\in [0; 2]$

MathCad

1

$$f(x,y) := \cos(x) + \sin(y).$$

2

$$x: xlow := 0 \quad xh \quad gh := 2.$$

3

$$: xn := 20.$$

4

$$: ylow := 0,$$

$$yh \quad gh := 2.$$

5

y,

$$: yn := 20.$$

6

$$: i := 0..xn - 1.$$

7

$$x \quad nd := xlow + i \cdot (xh \quad gh - xlow) / (xn - 1).$$

8

$$j: j := 0..yn - 1.$$

9

y:

$$y \quad nd_j := ylow + j \cdot (yh \quad gh - ylow) / (yn - 1).$$

10

$$: M_j := f(x \quad nd, y \quad nd_j).$$

11

MathCad

7.

$$f(x, y) := \cos(x) + \sin(y)$$

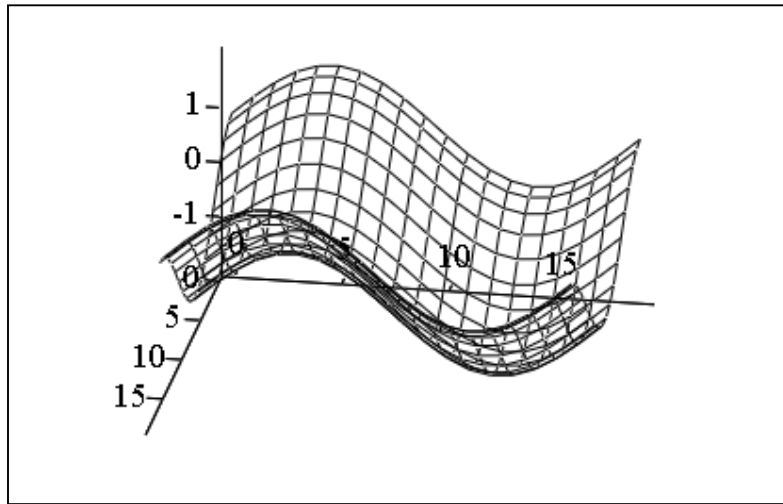
$$xlow := 0 \quad xhigh := 2 \cdot \pi \quad ylow := 0 \quad yhigh := 2 \cdot \pi$$

$$xn := 20 \quad yn := 20$$

$$i := 0..xn - 1 \quad j := 0..yn - 1$$

$$xind_i := xlow + i \cdot \frac{(xhigh - xlow)}{(xn - 1)} \quad yind_j := ylow + j \cdot \frac{(yhigh - ylow)}{(yn - 1)}$$

$$M_{i,j} := f(xind_i, yind_j)$$



M

7 -

4

- | | | | |
|----------|---------------|----------|--------------------|
| 1 | MathCad | Z | [-12 ; 4] |
| | 0,005. | | |
| 2 | | (" " |) - |
| ? | | | |
| 3 | | | - |
| ? | | | |
| 4 | MathCad | ? | |
| 5 | MathCad | | ? |

$m \times n$, $k = 1..n$, $m \times n$.

Calculator Toolbar /

Vector and

Matrx Toolbar – Determ nant /

();

Vector and

Matrx Toolbar - Matrx Transpose /

();

Vector and Matrx Toolbar – nverse /

().

Toolbars – Matrx /

()

Ctrl + ,


Matrx or Vector /

(Rows)

(Columns),

$$M := \begin{pmatrix} 0 & 1 & 3 & 5 \\ 2 & 4 & 6 & 8 \\ 7 & 9 & 11 & 10 \end{pmatrix}$$

2
Vector and Matrix Toolbar /

;
 , M1), M1

$$M1 := \begin{pmatrix} 1 & 2 & 3 \\ 7 & 0 & 9 \\ 4 & 5 & 6 \end{pmatrix} \quad |M1| = 48$$

3



$$M := \begin{pmatrix} 0 & 1 & 3 & 5 \\ 2 & 4 & 6 & 8 \\ 7 & 9 & 11 & 10 \end{pmatrix} \quad M^T = \begin{pmatrix} 0 & 2 & 7 \\ 1 & 4 & 9 \\ 3 & 6 & 11 \\ 5 & 8 & 10 \end{pmatrix}$$

4



1.

$$M1 := \begin{pmatrix} 1 & 2 & 3 \\ 7 & 0 & 9 \\ 4 & 5 & 6 \end{pmatrix} \quad M1^{-1} = \begin{pmatrix} -0.938 & 0.062 & 0.375 \\ -0.125 & -0.125 & 0.25 \\ 0.729 & 0.063 & -0.292 \end{pmatrix}$$

5

$$\begin{pmatrix} 1 & 2 & 3 \\ 7 & 0 & 9 \\ 4 & 5 & 6 \end{pmatrix} \cdot 5 = \begin{pmatrix} 5 & 10 & 15 \\ 35 & 0 & 45 \\ 20 & 25 & 30 \end{pmatrix}$$

6

()
 , + - ,
 ('), :

$$\begin{pmatrix} 1 & 2 & 3 \\ 7 & 0 & 9 \\ 4 & 5 & 6 \end{pmatrix} + \begin{pmatrix} -1 & 1 & 0 \\ 2 & -4 & 6 \\ 8 & 7 & 5 \end{pmatrix} = \begin{pmatrix} 0 & 3 & 3 \\ 9 & -4 & 15 \\ 12 & 12 & 11 \end{pmatrix}$$

()

$$M1 := \begin{pmatrix} 1 & 2 & 3 \\ 7 & 0 & 9 \\ 4 & 5 & 6 \end{pmatrix} \quad M2 := \begin{pmatrix} -1 & 1 & 0 \\ 2 & -4 & 6 \\ 8 & 7 & 5 \end{pmatrix} \quad M1 + M2 = \begin{pmatrix} 0 & 3 & 3 \\ 9 & -4 & 15 \\ 12 & 12 & 11 \end{pmatrix}$$

3.1

$$\begin{cases} a_{11} \cdot x_1 + a_{12} \cdot x_2 + \dots + a_{1n} \cdot x_n = b_1 \\ a_{21} \cdot x_1 + a_{22} \cdot x_2 + \dots + a_{2n} \cdot x_n = b_2 \\ \dots \\ a_{n1} \cdot x_1 + a_{n2} \cdot x_2 + \dots + a_{nn} \cdot x_n = b_n \end{cases},$$

1, 2, ..., xn.

(=),

() :

(det A = 0),

=

$$\begin{aligned} \cdot \cdot^{-1} &= \cdot^{-1} \\ \cdot^{-1} \cdot &= \cdot^{-1} \\ 1 \cdot &= \cdot^{-1} \\ &= \cdot^{-1}. \end{aligned}$$

5

$$\begin{cases} 3 \cdot x_1 + 4 \cdot x_2 = 180 \\ 4 \cdot x_1 + 5 \cdot x_2 + x_3 = 255 \\ 2 \cdot x_1 + 3 \cdot x_2 + 3 \cdot x_3 = 200 \end{cases}$$

1

,

– (Columns) 3).

– (Rows) 3

:

$$A := \begin{pmatrix} 3 & 4 & 0 \\ 4 & 5 & 1 \\ 2 & 3 & 3 \end{pmatrix}$$

2

$$: \begin{pmatrix} 180 \\ 255 \\ 200 \end{pmatrix}$$

3

,

,

:

$$|A| = -4$$

4

$$A^{-1} = \begin{pmatrix} -3 & 3 & -1 \\ 2.5 & -2.25 & 0.75 \\ -0.5 & 0.25 & 0.25 \end{pmatrix}$$

5

-1

:

$$X := A^{-1} \cdot B \quad X = \begin{pmatrix} 25 \\ 26.25 \\ 23.75 \end{pmatrix}$$

$$A \cdot X = \begin{pmatrix} 180 \\ 255 \\ 200 \end{pmatrix}$$

- 1 MathCad -
- 2 MathCad -
- 3 MathCad ?
- 4

4

f (n + 1)

$x_0, x_1, \dots, x_n,$

(. 1).

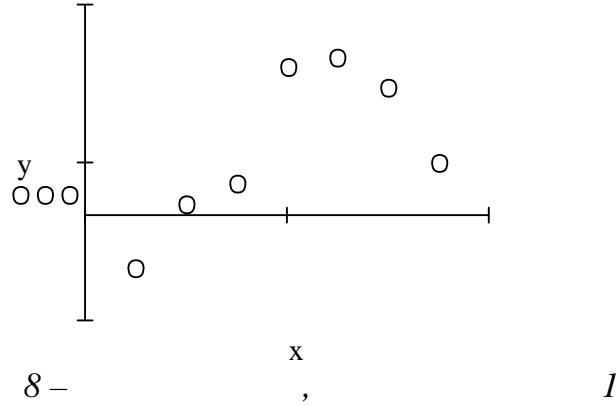
l

X	x_0	x_1	...	x_n
Y	y_0	y_1	...	y_n

(.8).
 $(n + 1)$

n:

$$P_n(x) = a_0 + a_1 \cdot x + a_2 \cdot x^2 + \dots + a_n \cdot x^n.$$



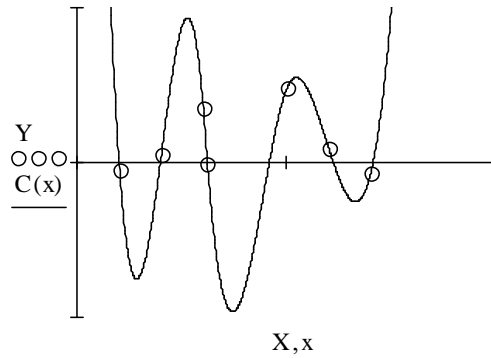
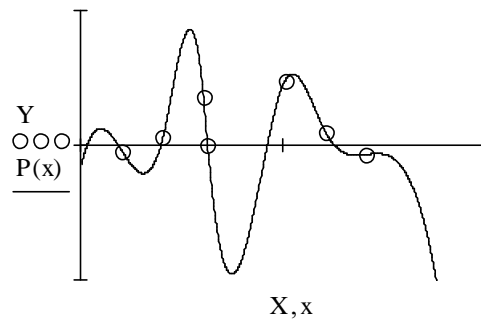
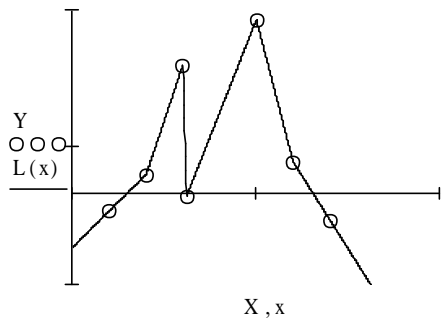
$(= 0..n)$
f $F(x) \approx P_n(x)$
P_n(x),
f $(= 0..n).$

$$F(x) \approx P_n(x) = a_0 + a_1 \cdot x + a_2 \cdot x^2 + \dots + a_n \cdot x^n$$

n = 1 , **n = 2** - , **n = 3** -
 (.9 ; 9 ; 9) .

$[x_0; x_n]$,
 $[x; x_{+1}]$

$[x_0; x_n]$ -



9 -

4.1

: [4; 4], [2; 2], [1; 3], [3; 5].

VX (), -
VY - .

$$VX := \begin{pmatrix} 1 \\ 2 \\ 3 \\ 4 \end{pmatrix} \quad VY := \begin{pmatrix} 3 \\ 2 \\ 4 \\ 5 \end{pmatrix}$$

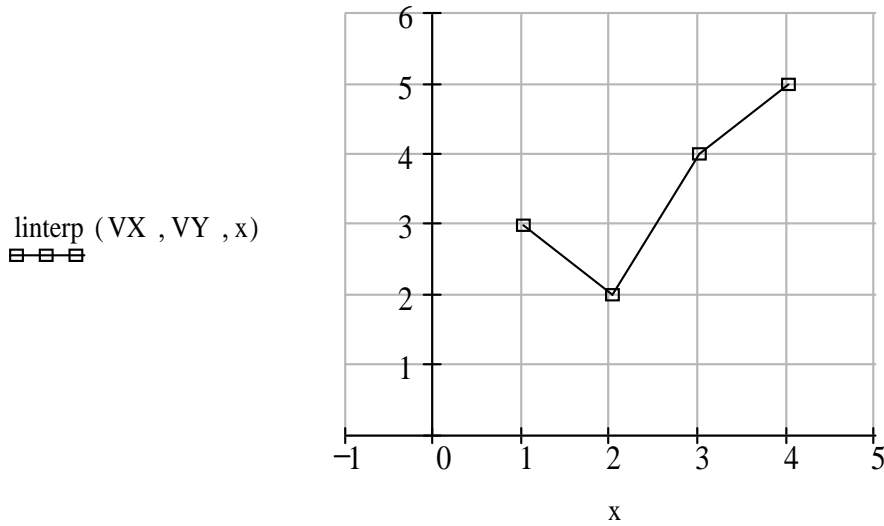
, , 2,5 1,2, -
L nterp (VX, VY, 2,5) = , : 3.

: **L nterp (VX, VY, 1,2) = 2,8.**

(
) (. 10).

$$\mathbf{VX} := \begin{pmatrix} 1 \\ 2 \\ 3 \\ 4 \end{pmatrix} \quad \mathbf{VY} := \begin{pmatrix} 3 \\ 2 \\ 4 \\ 5 \end{pmatrix}$$

$$\text{linterp}(\mathbf{VX}, \mathbf{VY}, 1.5) = 2.5 \quad \text{linterp}(\mathbf{VX}, \mathbf{VY}, 2.5) = 3 \quad \text{linterp}(\mathbf{VX}, \mathbf{VY}, 3.5) = 4.5$$



10 -

4.2 ()

nterp. (cspl ne) : VS := cspl ne (VX, VY).

VS (nterp) : f(x) := nterp (VS, VX, VY, x).

VX VY.

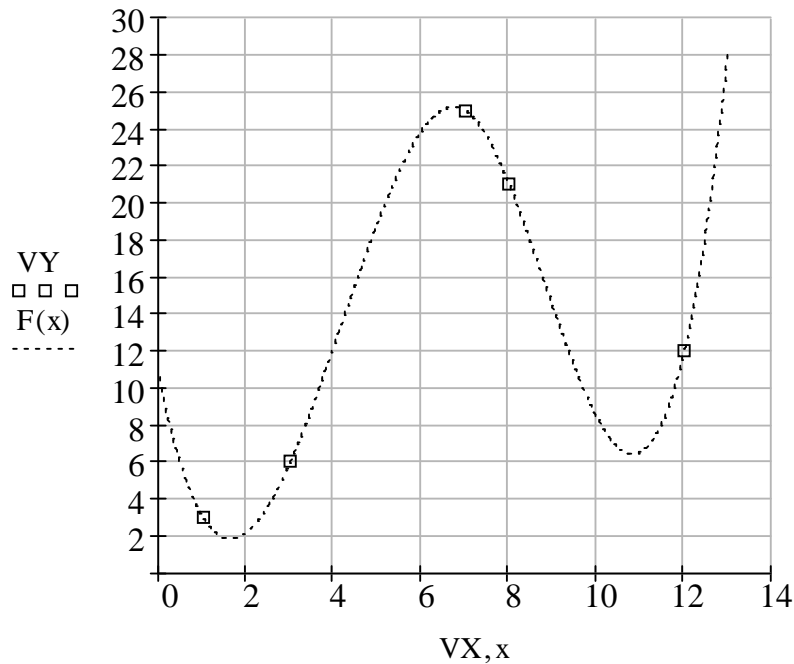
1 [1; 3], [7; 25] [12; 15] [3; 6] [8; 21] VS VY ():

$$VX := \begin{pmatrix} 1 \\ 3 \\ 7 \\ 8 \\ 12 \end{pmatrix} \quad VY := \begin{pmatrix} 3 \\ 6 \\ 25 \\ 21 \\ 12 \end{pmatrix}$$

2 : VS := cspline (VX, VY).
 3 , : F(x) := ninterp (VS, VX, VY, x).
 4 x = 2 -
 : F(2) =, 2,191.

$$VX := \begin{pmatrix} 1 \\ 3 \\ 7 \\ 8 \\ 12 \end{pmatrix} \quad VY := \begin{pmatrix} 3 \\ 6 \\ 25 \\ 21 \\ 12 \end{pmatrix} \quad x := 0, 0.01 .. 13$$

VS := cspline (VX, VY) F(x) := ninterp (VS, VX, VY, x) F(2) = 2.191



11 -

(. 11)

[0; 13], 0,01.

1

2

3

4

MathCad,

, , ?

MathCad,

MathCad,

5

5.1

Calculus Toolbar – Summat on /

().

$$\sum_{i=1}^n$$

Ctrl + Shift + 3 (Calculus Toolbar - iterated Product /



6

$$n := 1 .. 40 \quad x_n := \sin(0.1 \cdot n \cdot \pi)$$

$$\sum_{n=1}^{20} n = 210 \quad \sum_{n=1}^{10} x_n = 6.314 \quad \sum_{n=0}^{40} x_n \cdot n = -126.275$$

$$\prod_{n=0}^{20} (n + 1) = 5.109 \times 10^{19} \quad \sum_{n=0}^5 \sum_{m=0}^{10} n^m = 1.37 \times 10^7$$

1. MathCad

$$1 \quad 3 \quad 0,5, \quad = 1 + 1,5 + 2 + 2,5 + 3.$$

Shift + \$ (

Calculus Toolbar - Range Variable Summation /



Σ

MathCad

7

$$i := 1, 2 \dots 3$$

$$\sum_i i = 22$$

$$k := 0, 2 \dots 10$$

$$\sum_k k^2 = 220$$

5.2

1 $() = x^3$ $x = 2,$

2

$x + \text{Shift} + :$ $2,$ $x := 2.$

Calculus Toolbar



3

$x \cdot \frac{d}{dx}$

4

d / dx x^3

5

$=,$ $:$

$$x := 2$$

$$\frac{d}{dx} x^3 = 12$$

MathCad.

8

1) :

2) $^5 = 2,$

3) $^5 = 2 \cdot 10,$

$^5 = 2 = 10.$

$$x := 2 \quad y := 10$$

$$\frac{d}{dx}x^5 = 80 \quad \left(\frac{d}{dx}x^5\right) \cdot 10 = 800 \quad \frac{d}{dy}x^5 \cdot y = 32$$

$$3 \cdot x^2, \quad x^3, \quad x = 2, \quad 3 \cdot x^2,$$

5.3

(n-)

MathCad

$$() = x^9 \quad x \quad x = 2,$$

1
2
x. x:= 2.

Calculus Toolbar



$$\frac{d^1}{dx^1}$$

3
x.

$$\frac{d^1}{dx^1}$$

4
3.

$$\frac{d^3}{dx^3}$$

$d/dx \quad x^9$

=,

$$\frac{d^3}{dx^3} x^9 = 3.226 \cdot 10^4$$

$n = 1$

$n = 0$

5.4

MathCad

$$= \sin(x^2) \quad 0 \quad \pi / 4$$

1
Toolbar



Calculus

$$\int_a^b \quad d$$

2

0.

$\pi / 4$.

$$\int_0^{\pi/4} \quad d$$

3
 $\sin(x^2)$.

d.

4

d x.

=

$$\int_0^{\frac{\pi}{4}} \sin(x^2) dx = 0.157$$

- 1 MathCad -
- 2 MathCad -

6

MathCad,

P: = M n m ze (< ' >,< >),
 P: = Max m ze (< ' >,< >),
 P - ' .

nsert - Funct on - Funct on Category

(Solv ng) - Funct on Name (M n m ze, Max m ze) / - -
 (') - (M n m ze, Max m ze)

nsert Funct on .

9

$x \quad y,$

$$f(x,y) = x^2 + y^2 + 3$$

:

1

$$f(x,y) := x^2 + y^2 + 3.$$

2

$$x := 1$$

$$y := 1.$$

3

$$P := \text{Minimize}(f, x, y).$$

4

$$P = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$= 1 \quad = 0.$$

MathCad:

$$f(x, y) := (x - 1)^2 + y^2 + 3 \quad x := 1 \quad y := 1$$

$$P := \text{minimize}(f, x, y)$$

$$P = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

10

$$z(x) = x - 5 - x - 7x + 3$$

:

1

$$z(x) := x - 5 - x - 7x + 3$$

2

$$x := 0.$$

3

$$P := \text{Maximize}(z, x).$$

4

$$P = -0,429.$$

5

$$z(P) = 5.$$

6

:

$$\frac{d}{dx}z(P) = 0$$

MathCad:

$$z(x) := |x - 5| - |x| - |7 \cdot x + 3|$$

$$x := 0 \quad P := \text{Maximize} \quad (z, x)$$

$$P = -0.429 \quad z(P) = 5$$

$$\frac{d}{dx}z(P) = 0$$

11

$$f(x, y) = x^2 + y^2 \quad x \in [-10, 10]$$

$y \in [10, 20]$.

:

1

$$f(x, y) := x^2 + y^2.$$

2

$x := 1; y := 1.$

3

G ven.

4

:

$$x \quad -10 \quad 10;$$

$$y \quad 10 \quad y \quad 20.$$

5

$$P := \text{Minimize} (f, x, y).$$

6

,

:

$$P = \begin{pmatrix} -2.662 \times 10^{-15} \\ 10 \end{pmatrix}$$

$$, \quad = 0 \quad = 10.$$

7

$$: f(0; 10) = 100.$$

MathCad

:

$$f(x, y) := x^2 + y^2 \quad x := 1 \quad y := 1$$

given

$$x \geq -10 \quad x \leq 10 \quad y \geq 10 \quad y \leq 20$$

$$P := \text{Minimize} \quad (f, x, y)$$

$$P = \begin{pmatrix} -2.662 \times 10^{-15} \\ 10 \end{pmatrix}$$

$$f(0, 10) = 100$$

, 11

Solve Block,

Given.

200. **Solve Block**

<, ≤, >, ≥, =

≠.

1

MathCad,

?

2

MathCad

?

3

(Solve Block)?

7.1

MathCad root, insert Function - Function Category (Solving) -

Function Name (root) / () - (root)

: root(f(x), x).

f(x) (,) -

root. x -

(,)

), root

()

. MathCad

, ,

root f(x)

, e^x = x³.

:

1 ,

x³ - e^x = 0.

f(x) root.

2 () = x³ - e^x.

, - 2

5.

3 1 2 ,

root.

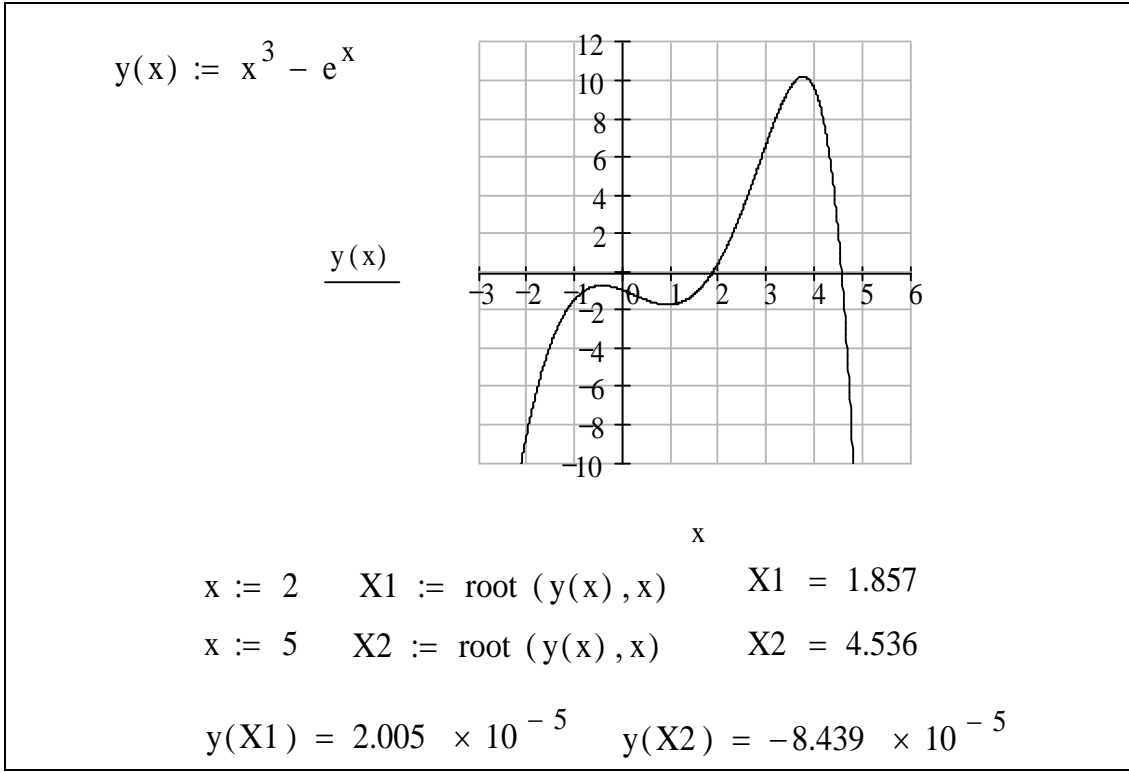
4

5 , -

12.

root :

- ()
root;
- , $x^2 - 1 = 0$,
; ;
- **root** , ;
- , $f(x) = g(x)$
f (x) - g (x) = 0 . **root**
: root (f (x) - g (x), x).



12- , root

7.2

$$P_n(x) = a_n X_n + \dots + a_2 X_2 + a_1 X_1 + a_0$$

polyroots,
root. **root** **polyroots**
polyroots

: polyroots(v), v

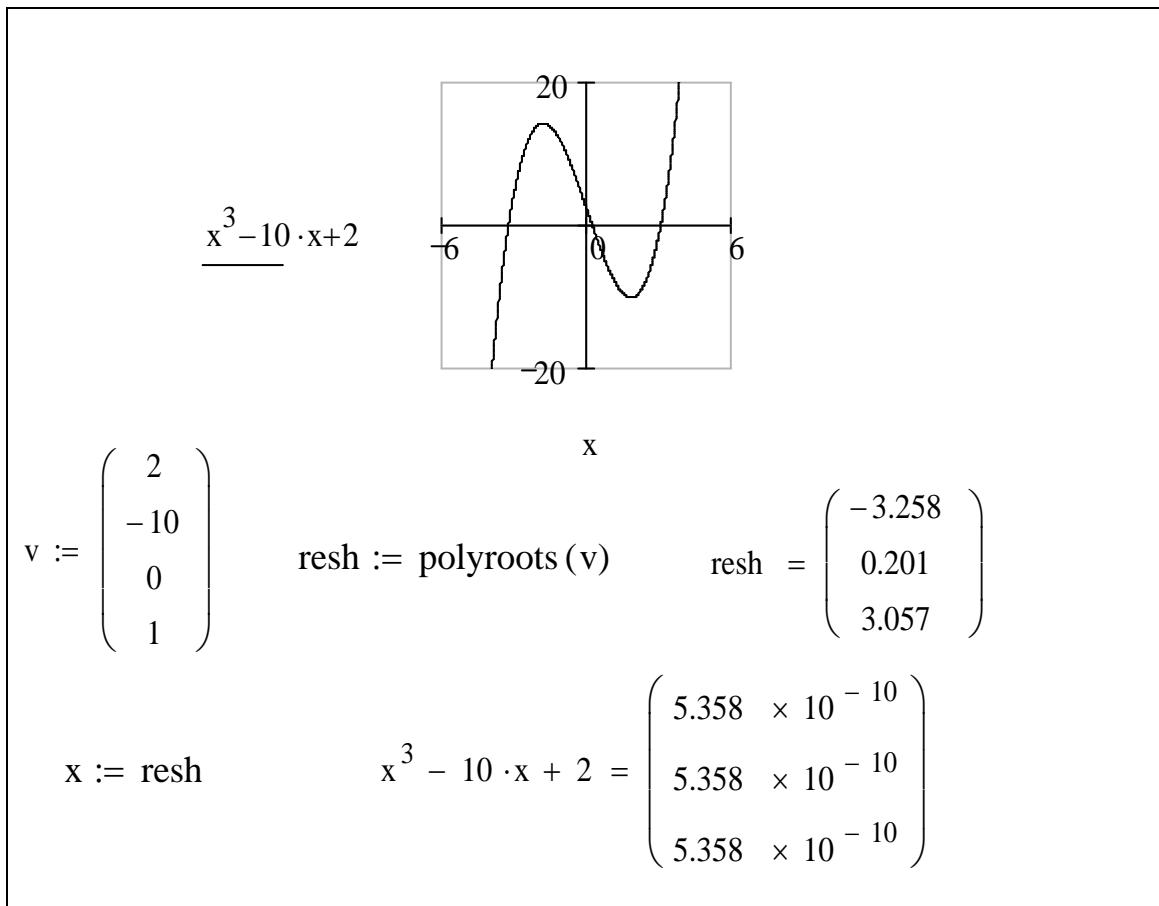
(n+1):

$$v := \begin{pmatrix} A_0 \\ A_1 \\ A_2 \\ \dots \\ A_n \end{pmatrix}$$

13

polyroots

$$x^3 - 10 \cdot x + 2 \cdot x^0.$$



13 -

polyroots

7.3

MathCad

1

(MathCad

2

G ven.

3

G ven.

= ().

trl + =

Boolean Toolbar - Equal to /

().

: <, >, ≤ ≥..

F nd.

F nd

F nd (z1, z2, z3, ...) –

F nd

G ven

F nd.

F nd

, **F nd (z1, z2)**

z1 z2

G ven,

F nd,

G ven

F nd (

x y

z w –

- w = z (=

trl + = –

) 1,

– 0;

- x > y (>

>) –

- x < y (<

<) –

- $x \geq y$ (\geq **trl + 0**) -
 ;
 - $x \leq y$ (\leq **trl + 9**) -
 .

- \neq (\neq **trl + 3**) - ;

- ;
 - **a < b < c.**

F nd : x y

, athcad , ?

found / , **F nd** : **No solut on was**

athcad , **F nd** **Minerr.**

1 MathCad ,

2 , ?

3 MathCad -

, ?

4 ,

MathCad?

MathCad

13

: rkf xed -

- 4-

$h^5, h -$

:

Z: = rkf xed (y, x1, x2, npo nts, D),

y -

x1 -

x2 -

npo nts -

D -

rkf xed

nsert -

Funct on -D fferent al Equat on Solv ng - rkf xed /

- rkf xed

nsert Funct on /

).

MathCad.

12

$$y'' + 3y = 0, y(0) = 1, y'(0) = 0.$$

D.

$$\begin{cases} y' = y_1 \\ y'' = -3y_0 \end{cases}$$

$$y' = y_1; y = y_0.$$

$$D = \begin{bmatrix} y_1 \\ -3 \cdot y_0 \end{bmatrix}.$$

$$y = \begin{bmatrix} y(0) \\ y'(0) \end{bmatrix},$$

$$y = \begin{bmatrix} 1 \\ 0 \end{bmatrix}.$$

13

$$y'' + 3y = x^2 + 3, y(0) = 1, y'(0) = 0.$$

$$D = \begin{bmatrix} y_1 \\ x^2 + 3 - 3 \cdot y_0 \end{bmatrix},$$

14

$$\mathbf{y}''' + 2 \cdot \mathbf{y}'' + \sin(\mathbf{x}) \cdot \mathbf{y}' - \mathbf{x} \cdot \mathbf{y} = 13,$$

$$\mathbf{y}(0) = 1, \mathbf{y}'(0) = 0, \mathbf{y}''(0) = -1$$

$$\mathbf{D} = \begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \\ 13 - 2 \cdot \mathbf{y}_2 - \sin(\mathbf{x}) \cdot \mathbf{y}_1 + \mathbf{x} \cdot \mathbf{y}_0 \end{bmatrix},$$

$$: \quad \mathbf{y} = \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}.$$

rkf xed

+ 1
, n -

	0	1	2	...
0	0	(0)	'(0)	...
1	1	(1)	'(1)	...
2	2	(2)	'(2)	...
...

, - (), -
: '(), ''() . . .

15

,

$$\mathbf{y}'' = -\mathbf{y}' + 2 \cdot \mathbf{y}$$

$$: \mathbf{y}(0) = 1, \mathbf{y}'(0) = 3.$$

,

$$\mathbf{y} = \begin{bmatrix} 1 \\ 3 \end{bmatrix} -$$

$$\mathbf{x1} = 0, \mathbf{x2} = 2 -$$

$$\text{npoints} = 400 -$$

$$\mathbf{D}(\mathbf{x}, \mathbf{y}) = \begin{bmatrix} \mathbf{y}_1 \\ -\mathbf{y}_1 + 2 \cdot \mathbf{y}_0 \end{bmatrix} -$$

Matr x Toolbar – Subscr pt /



MathCad:

$$y := \begin{pmatrix} 1 \\ 3 \end{pmatrix}$$

$$D(x, y) := \begin{pmatrix} y_1 \\ -y_1 + 2 \cdot y_0 \end{pmatrix}$$

$$Z := \text{rkfixed}(y, 0, 2, 400, D)$$

[0;2], - 400 -
(. 14).

$$Z^{<0>}$$

Vector and Matrix Toolbar



$$- Z^{<1>}$$

(. 15).

1

MathCad,

2

3

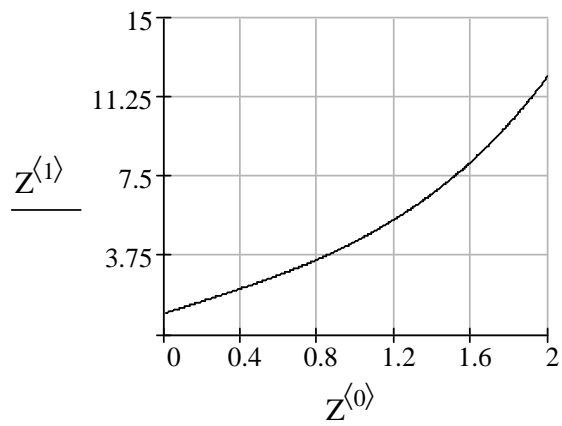
rkf xed

4

?

	0	1	2	
24	0.12	1.355	2.928	
25	0.125	1.369	2.927	
26	0.13	1.384	2.926	
27	0.135	1.399	2.925	
28	0.14	1.413	2.925	
29	0.145	1.428	2.924	
30	0.15	1.443	2.924	
31	0.155	1.457	2.924	
32	0.16	1.472	2.924	
33	0.165	1.486	2.924	
34	0.17	1.501	2.925	
35	0.175	1.516	2.925	
36	0.18	1.53	2.926	
37	0.185	1.545	2.926	
38	0.19	1.56	2.927	
39	0.195	1.574	2.928	

14 -



15 -

,
 : , ,
 ,
 . . .
 ,
 .

2.

2

1	,	.
2	,	.
3		,

, ,
 n : x_1, x_2, \dots, x_n (, n).

$$\begin{aligned}
 & : \bar{x}^* = \frac{1}{n} \sum_i x_i, \\
 & : D^* = \frac{1}{n} \sum_i (x_i - \bar{x}^*)^2, \\
 & : \sigma^* = \sqrt{D^*}, \\
 & : Sk = \frac{1}{(\sigma^*)^3} \cdot \frac{1}{n} \sum_i (x_i - \bar{x}^*)^3, \\
 & : Ex = \frac{1}{(\sigma^*)^4} \cdot \frac{1}{n} \sum_i (x_i - \bar{x}^*)^4 - 3.
 \end{aligned}$$

\bar{x}^*

16

(.3)

3

1.67	2.41	0.79	1.41	2.50	2.29	2.58	1.32
3.75	1.94	0.95	3.48	2.39	1.17	1.92	1.04
2.13	1.58	2.18	2.30	3.03	1.50	2.53	1.91
1.31	3.62	1.49	1.98	2.14	3.35	2.89	2.51
2.31	2.34	1.00	2.03	0.64	2.67	0.09	1.78
3.24	1.91	1.20	1.61	2.35	1.73	2.93	2.32
2.84	1.29	2.28	2.54	1.85	2.40	2.22	2.90
2.37	2.68	2.00	2.70	2.33	2.86	0.36	1.98
2.53	0.80	2.89	0.73	1.01	1.85	2.05	1.16
1.76	2.78	2.43	1.85	1.21	1.53	1.54	2.43

1 (,
fio_2.dat).

2 : , n,

mean, $R = x_{min} - x_{max}$,

, Sk, Ex.

3 , ,
10. ,

4 : $P(2,1 < X < 3,2) = ?$.

5 ,
10% ,


```

1                                     dan.dat.
2                                     : ' n,
mean,                               R = xmin - xmax,
, Sk,                               Ex :

```

```
ORIGIN:= 1
```

```
i:= 1 .. 80
```

```
xi:= READ ("dan.dat")
```

```
xmax:= max( ) xmin:= min( ) xmax = 3.75xmin = 0.09
```

```
xi:= sort( ) n:= length( ) n = 80 R:= xmax - xmin
```

```
mean:= mean( ) mean = 2.03
```

```
disp:= var( ) * n / (n - 1) disp = 0.574
```

```
sigma:= sqrt(disp) sigma = 0.758
```

```
mu3:= (1/n) * sum(xi - mean)^3 mu4:= (1/n) * sum(xi - mean)^4
```

```
Sk:= mu3 / sigma^3 Sk = -0.173
```

```
Ex:= (mu4 / sigma^4) - 3 Ex = -0.288
```

```

3                                     ,
10.

```

```
m:= 10 h := R / m h = 0.366
```

```
j:= 1 .. m k:= 1 .. m - 1
```

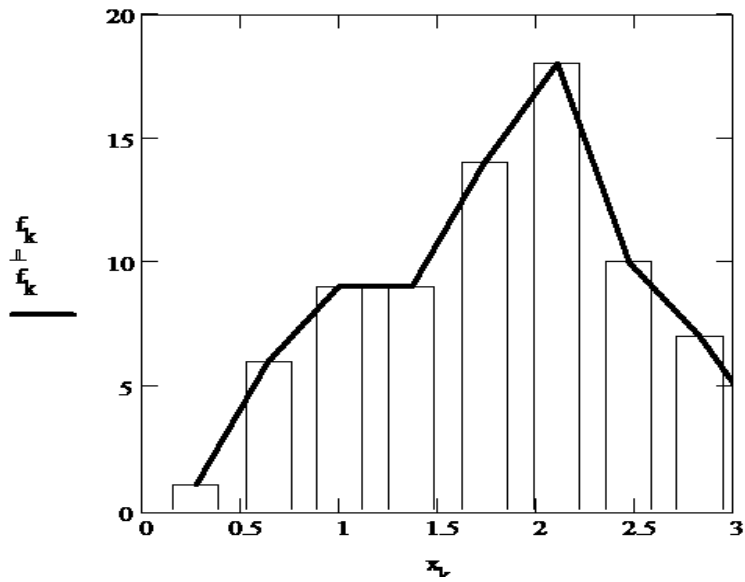
```
xj:= xmin + (h/2) * (2 * j - 1)
```

```
f := hist(x, xi)
```

```

,
( . 16)

```

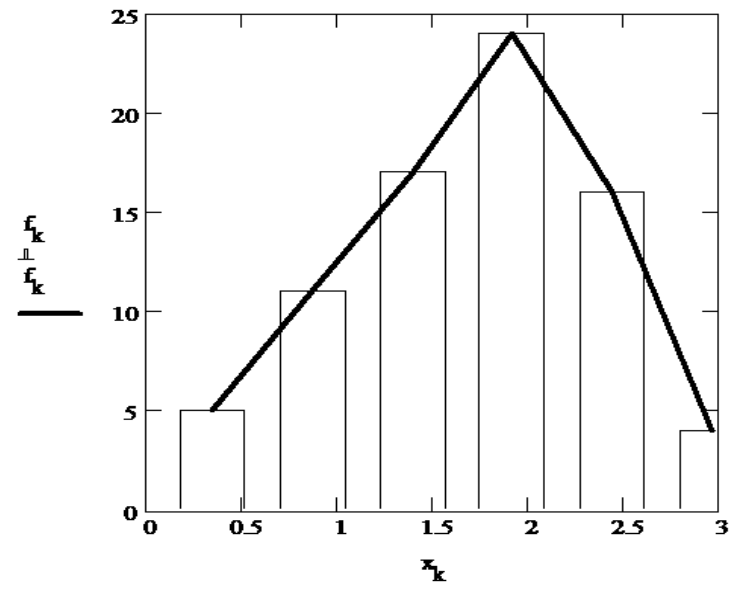


16 -

10

7

(. 17).



17 -

7

4

(a, b)

$$P(a < X < b) = F(b) - F(a),$$

$F(x)$ -

$\text{pnorm}(x, \text{mean}, \sigma)$.

$$\text{pnorm}(3.2, \text{mean}, \sigma) - \text{pnorm}(2.1, \text{mean}, \sigma) = 0.402;$$

$$P(2.1 < X < 3.2) = F(3.2) - F(2.1) = 0.402.$$

5

\bar{x}

$$\delta = 0.1 \cdot \bar{x} = 0.1 \cdot 2.03.$$

$$P(|x - \bar{x}| < \delta) = 2F\left(\frac{\delta}{\sigma}\right).$$

$$\delta := 0.1 \cdot \text{mean}$$

$$\delta = 0.203$$

$$2 \cdot \text{pnorm}\left(\frac{\delta}{\sigma}, \text{mean}, \sigma\right) = 0.02$$

:

$0.1\bar{x}$

$$0.02 \cdot 100\% = 2\%$$

1

:

'

,

,

,

,

,

.

2

?

3

?

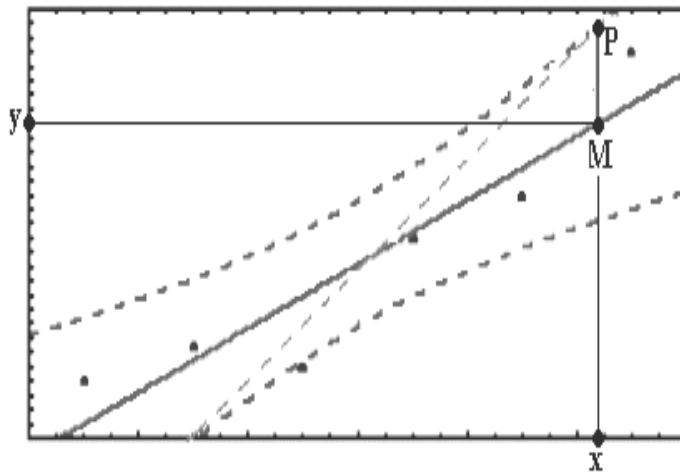
4

5

$$y = b_0 + b_1x$$

. 19

$$y: y = b_0 + b_1x + \epsilon$$



18 -

= 0,99 (95%, 99%).

$$y = b_0 + b_1x + \epsilon$$

= 0,95

. 18

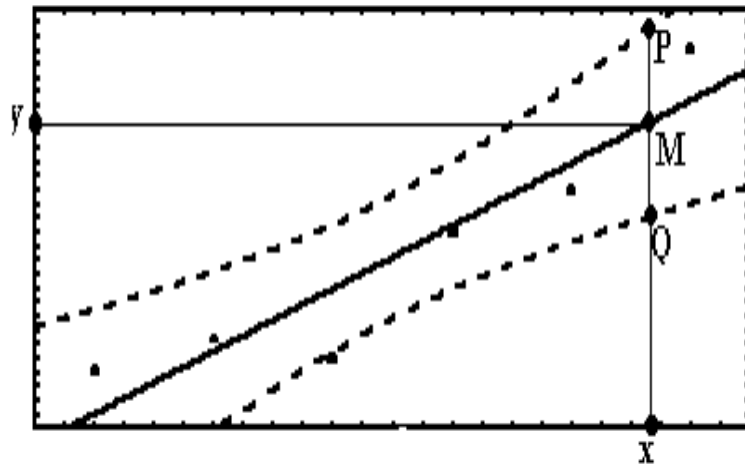
$$b_0 + b_1x.$$

y =

PQ (.19).

$$\delta = MP = MQ.$$

$$O . . = \left| \frac{\delta}{y} \right| \cdot 100\%.$$



19 -

17

(.4)

4

	X	Y
1	7,89	8,9
2	14,41	4,3
3	6,01	10,2
4	9,17	4,9
5	6,78	8,3
6	8,91	7,8
7	6,17	13,1
8	10,11	4,9
9	5,98	13,3
10	6,10	10,7
11	5,90	13,7
12	8,13	5,6
13	9,01	4,7
14	6,00	11,1
15	6,13	10,8

1

2

80%, 95% 99%

3

4

,
(80%, 95%, 99%),

5

δ_γ ,

(80%, 95%, 99%): δ_{80} δ_{95} δ_{99} .

6

()

(80%, 95%, 99%)

$$\left| \frac{\delta_\gamma}{y} \right| \cdot 100\% (\delta_\gamma (y) \text{ }).$$

7

%

1

dan_x.dat

dan_y.dat.

2 MathCad

:

ORIGIN := 1 N := 15 i := 1..N

$x_i := \text{READ}(\text{"dan_x.dat"})$

$$x^T =$$

	1	2	3	4	5	6	7	8	9	10
1	7.89	14.41	6.01	9.17	6.78	8.91	6.17	10.11	5.98	6.1

$y_i := \text{READ}(\text{"dan_y.dat"})$

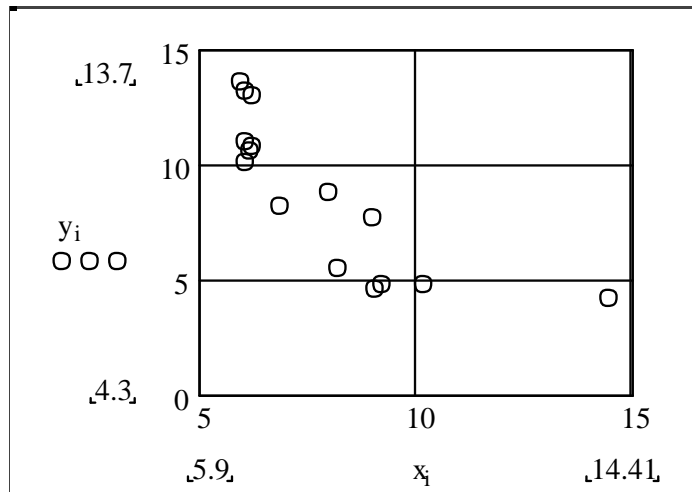
$$y^T =$$

	1	2	3	4	5	6	7	8	9	10
1	8.9	4.3	10.2	4.9	8.3	7.8	13.1	4.9	13.3	10.7

(. 20).

y

: corr(x,y) = -0.808 ■



20 -

X Y -0,808.

$0,6 < |-0,808| < 0,9$,

$y = b_0 + b_1x$:

$b_0 := \text{intercep}(x,y)$ $b_0 = 17.818$

$b_1 := \text{slope}(x,y)$ $b_1 = -1.157$

$y_{\hat{i}} := b_0 + b_1 \cdot x_i$

:

$X_{\text{mean}} := \text{mean}(x)$ $X_{\text{mean}} = 7.78$

Y:

$Y_{\text{mean}} := \text{mean}(y)$ $Y_{\text{mean}} = 8.82$

(Mean)

$(\bar{x}, \bar{y}) = (7.78, 8.82)$.

:

$$S2 := \left(\frac{1}{N-1} \right) \cdot \sum_{k=1}^N (y_k - \bar{y}_k)^2 \quad S2 = 3.88$$

$$X_{\min} \leq X \leq X_{\max},$$

:

$$X_{\min} = \min(x) \quad X_{\min} = 5.9 \quad X_{\max} = \max(x) \quad X_{\max} = 14.41$$

$$(X_{\min}; X_{\max}),$$

$$(5.9; 14.41).$$

$$80\%, 95\% \quad 99\%$$

MathCad

$$\gamma = 80\% \quad (.21)$$

$$\alpha := 0.20 \quad t := qt \left[1 - \left(\frac{\alpha}{2} \right), N - 2 \right]$$

$$\delta_i := t \cdot \sqrt{S2} \cdot \sqrt{\left(\frac{1}{N} \right) + \frac{(x_i - \bar{x})^2}{\sum_{k=1}^N (x_k - \bar{x})^2}}$$

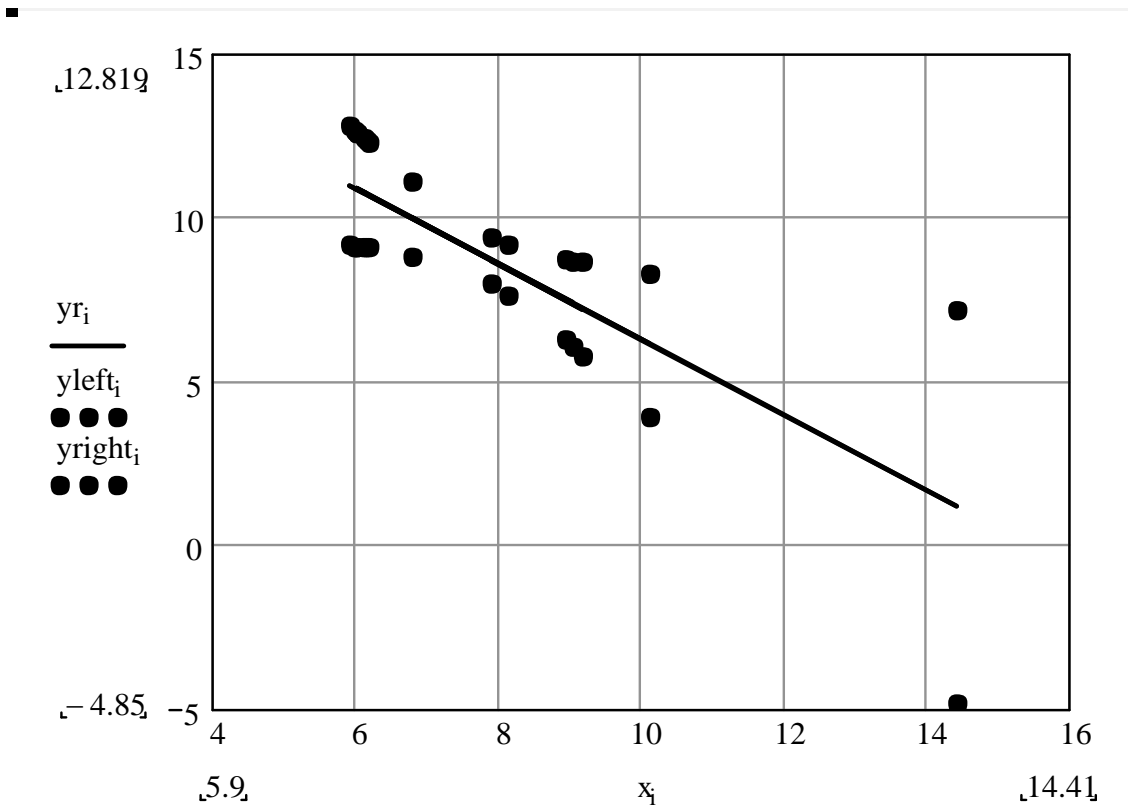
$$y_{\text{left}_i} := y_{r_i} - \delta_i \quad y_{\text{right}_i} := y_{r_i} + \delta_i$$

$$\gamma = 95\% \quad (.22).$$

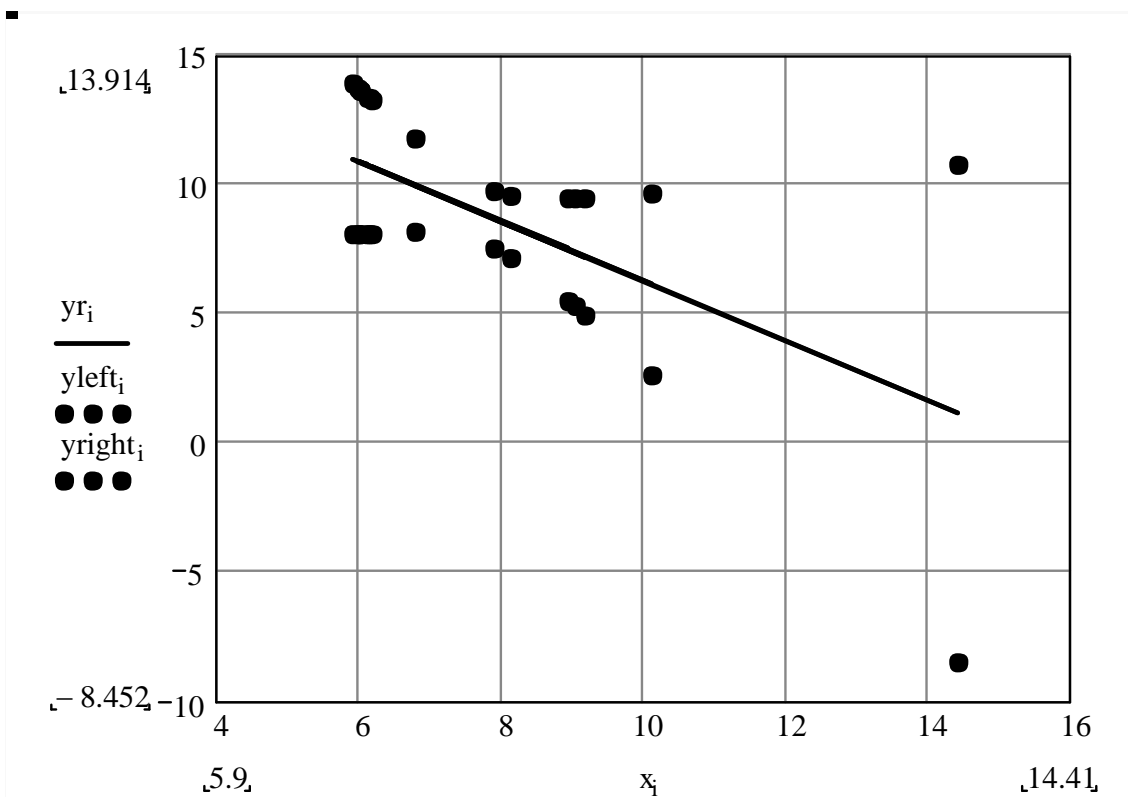
$$\alpha := 0.05 \quad t := qt \left[1 - \left(\frac{\alpha}{2} \right), N - 2 \right]$$

$$\delta_i := t \cdot \sqrt{S2} \cdot \sqrt{\left(\frac{1}{N} \right) + \frac{(x_i - \bar{x})^2}{\sum_{k=1}^N (x_k - \bar{x})^2}}$$

$$y_{\text{left}_i} := y_{r_i} - \delta_i \quad y_{\text{right}_i} := y_{r_i} + \delta_i$$



21



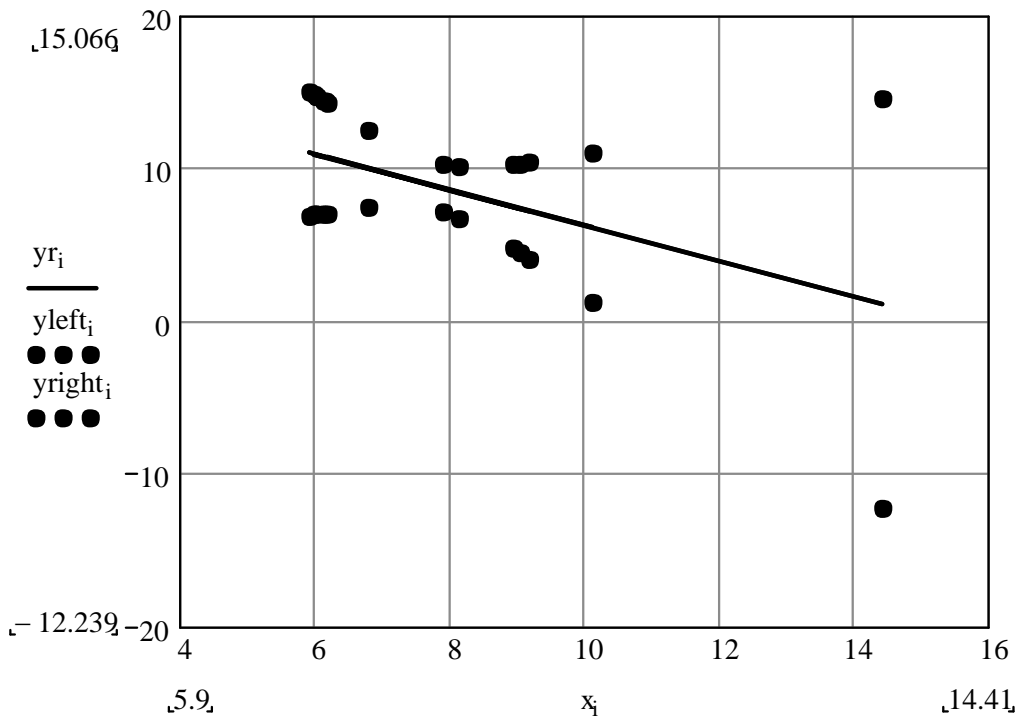
22

$$\gamma = 99\% \quad (.23).$$

$$\alpha := 0.01 \quad t := \text{qt} \left[1 - \left(\frac{\alpha}{2} \right), N - 2 \right]$$

$$\delta_i := t \cdot \sqrt{S^2} \cdot \sqrt{\left(\frac{1}{N} \right) + \frac{(x_i - X_{\text{mean}})^2}{\sum_{k=1}^N (x_k - X_{\text{mean}})^2}}$$

$$y_{\text{left}_i} := y_{r_i} - \delta_i \quad y_{\text{right}_i} := y_{r_i} + \delta_i$$



23

3-6

1

2

$\gamma?$

3

y

-

x?

4

?

5

?

6

,

-

?

1

$$f(x) = 3 + \sin(4 + x^2)$$

MathCad -

. ,
(
)
:
.

1

$$: f(x) := 3 + \sin(4 + x^2).$$

2

:

2.1

(-5;5)

0,1 (.)

Graph /

X-Y Plot /



2.2

- ,
) - y(x).
, , ,

Auto Gr g

Number of Gr ds

2

99 (10).

2.3

():

0,6,

2,4.

0,8

2,0.

2.4

:
) : f(0,6) = , f(0,8), f(2),

f(2,4)

2.5

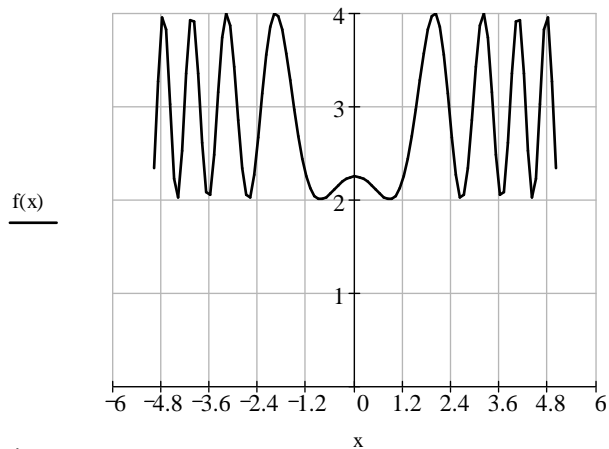
[0,6; 2,4], [0,8; 2,003] [2,0; 3,989],
[0,6; 2,061] [2,4; 2,671].

MathCad

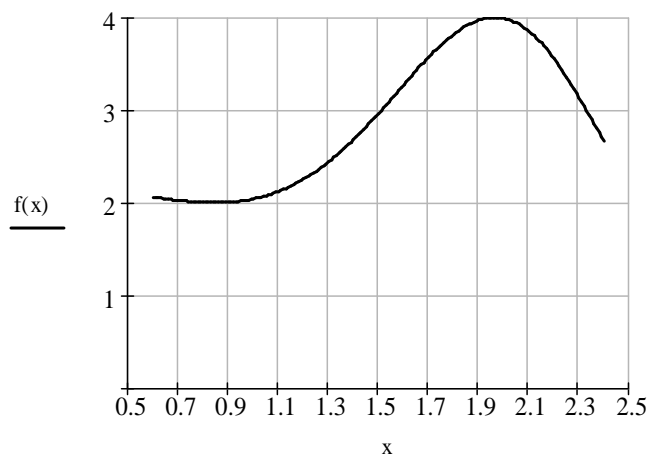
.1.

$$f(x) := 3 + \sin(4 + x^2)$$

$$x := -5, -4.9 .. 5$$



$$x := 0.6, 0.61 .. 2.4$$



$$f(0.6) = 2.061$$

$$f(0.8) = 2.003$$

$$f(2) = 3.989$$

$$f(2.4) = 2.671$$

.1 -

1

2

1 :

1 [x1; y1], [x2; y2], [x3; y3], [x4; y4], -

1,

.

.

:

$$. = \frac{\quad - \quad}{100} .$$

2 [x1; y1], [x2; y2], [x3; y3] [x4; y4]. -
 .1, . -
 . -
 . -
 3 .

, 1: [0,6; 2,061], [0,8; 2,003], [2,0; 3,989],
 [2,4; 2,671].

1 $f(x) = 3 + \sin(4 + x^2)$

[0,6; 2,4] 0,001.

1.1 :

1.1.2 : .

1.1.3 : .

1.1.4 ' , $F(x) := \text{interp}(X, Y, x)$.

1.1.5 . -

('), -

. .

1.1 :

1.1.1 , -

1,2.

:

$$\text{Otr}_P := |f(1.2) - F(1.2)| \cdot \frac{100}{f(1.2)}$$

1.2.3

Otr_Pogresh = 18,274%.

.2.

2 :

2.1 .

2.2 ,

vs = spline(X, Y) ' $F(x) := \text{interp}(vs, X, Y, x)$.

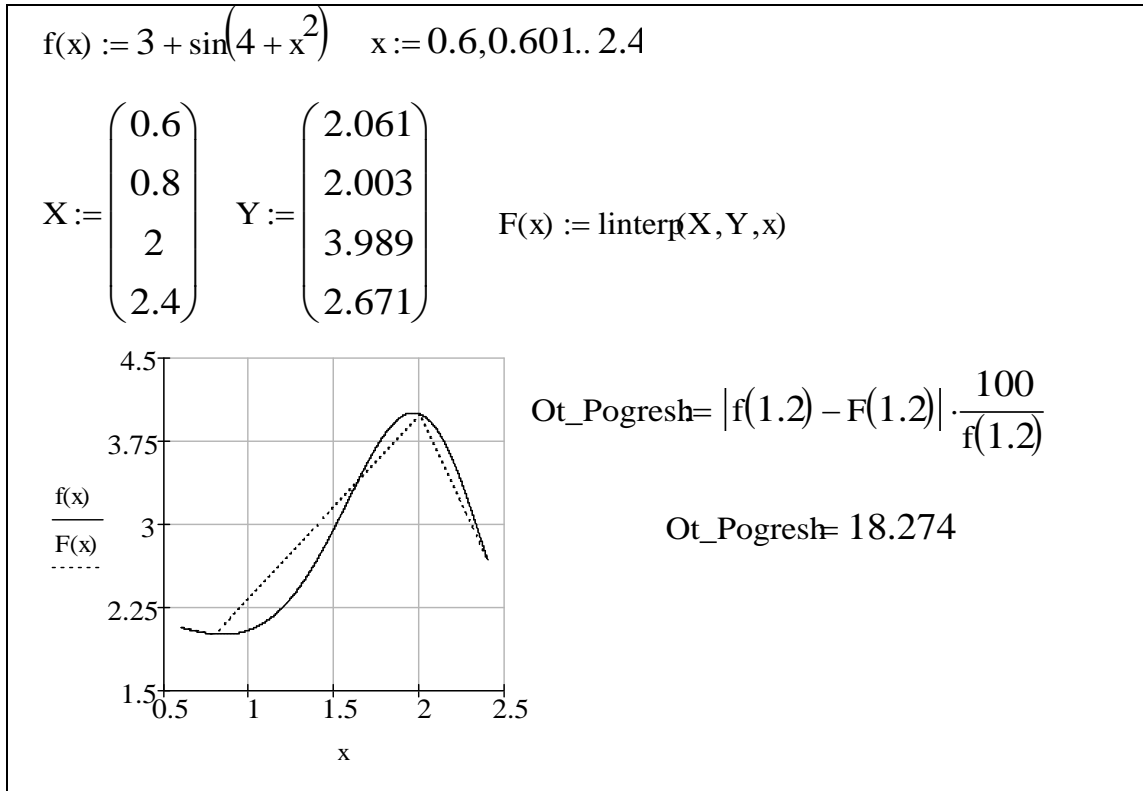
2.3

('),

. .

2.4

1,5.



.2 -

2.5

$$\text{Ot_Pogresh} := |f(1.5) - F(1.5)| \cdot \frac{100}{f(1.5)}$$

16,616%.

MathCad

.3.

3

$$P(x) = y + q \cdot y_0,$$

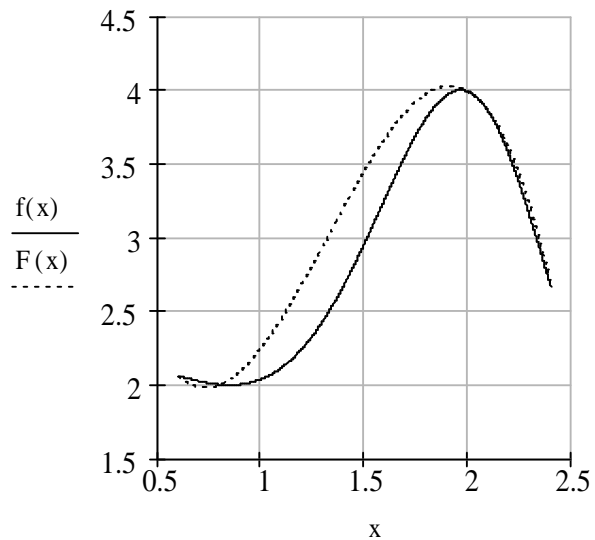
$$P(x) = y + q \cdot \Delta y_0 + \frac{q \cdot (q-1)}{2} \cdot \Delta^2 y_0 + \frac{q \cdot (q-1) \cdot (q-2)}{6} \cdot \Delta^3 y_0.$$

$$f(x) := 3 + \sin(4 + x^2) \quad x := 0.6, 0.601 \dots 2.4$$

$$X := \begin{pmatrix} 0.6 \\ 0.8 \\ 2 \\ 2.4 \end{pmatrix} \quad Y := \begin{pmatrix} 2.061 \\ 2.003 \\ 3.989 \\ 2.671 \end{pmatrix}$$

$$vs := \text{cspline}(X, Y)$$

$$F(x) := \text{interp}(vs, X, Y, x)$$



$$\text{Ot_Pogresh} := |f(1.5) - F(1.5)| \cdot \frac{100}{f(1.5)} \quad \text{Ot_Pogresh} = 16.616$$

.3 -

" "

,

,

-

.

,

,

$N \cdot y_0$

.

-

,

[18,274%]

[16,616%],

.

-

,

,

.

3

1 f(x) 1 (.2) . -

2 f(x) .1 (.2) . -

3 [x1, x4] , -

4 .1, -

5 -

I I :

1.1 :

$$f(x) := 3 + \sin(4 + x^2).$$

1.2 . :
1.2.1 , ' :

$$\frac{d}{dx}(3 + \sin(4 + x^2))$$

1.3 . :

1.3.1 . 1.2.1 ,

S mpl fy / **Symbol cs /** -
(-
MathCad) , -

1.3.2 -

(, , -

df(x) :

$$df(x) := 2 \cdot \cos(4 + x^2) \cdot x.$$

1.4 **d(x):**
 1.4.1 ,

$$\begin{aligned} df(0.6) &= -0.414 & df(2) &= -0.582 \\ df(0.8) &= -0.116 & df(2.4) &= -4.533 \end{aligned}$$

1.4.2 ,
d(x) := lnterp (X, Y, x).

1.4.3 -
 . , -

1,6.

1.4.5 :

$$\text{Ot_Pogresh} := |df(1.6) - dF(1.6)| \cdot \frac{100}{f(1.6)}$$

107,074%.

MathCad .4.

2 2 :

2.1 , 1.1 - 1.3, 1.4.1 3.

2.2 **vs := csplnc (X, Y).**

2.3 **dF (x) := nterp (vs, X, Y, x).**

2.4 ,

1,6.

69,034 %.

MathCad .5.

3 3 :

3.1 **f (x) := 3 + s n (4 + x2).**

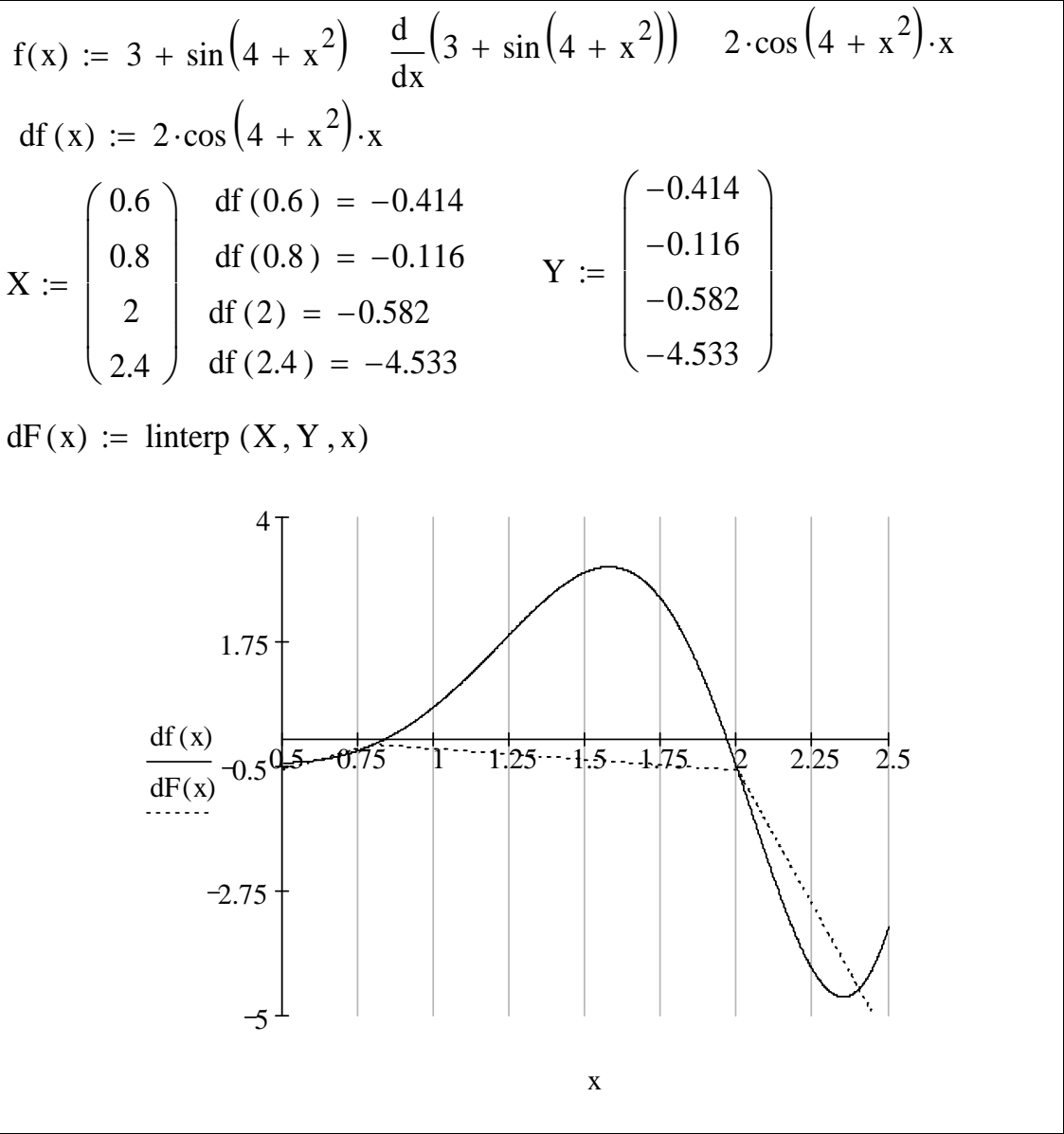
3.2 **X:= Y:= .**

3.3 **F1 (x) := lnterp (X, Y, x),**

vs := csplnc (X, Y)

Fk (x) := nterp (vs, X, Y, x).

3.4 **f (x), :**



.4 -

3.4.1

**Calculus Toolbar /
Def n te ntegral /**



3.4.2

=.

5,418.

3.5

F1 (x)

Fk(x).

5,541 5,786,

3.6

MathCad

.6.

$$f(x) := 3 + \sin(4 + x^2) \quad \frac{d}{dx}(3 + \sin(4 + x^2)) \quad 2 \cdot \cos(4 + x^2) \cdot x$$

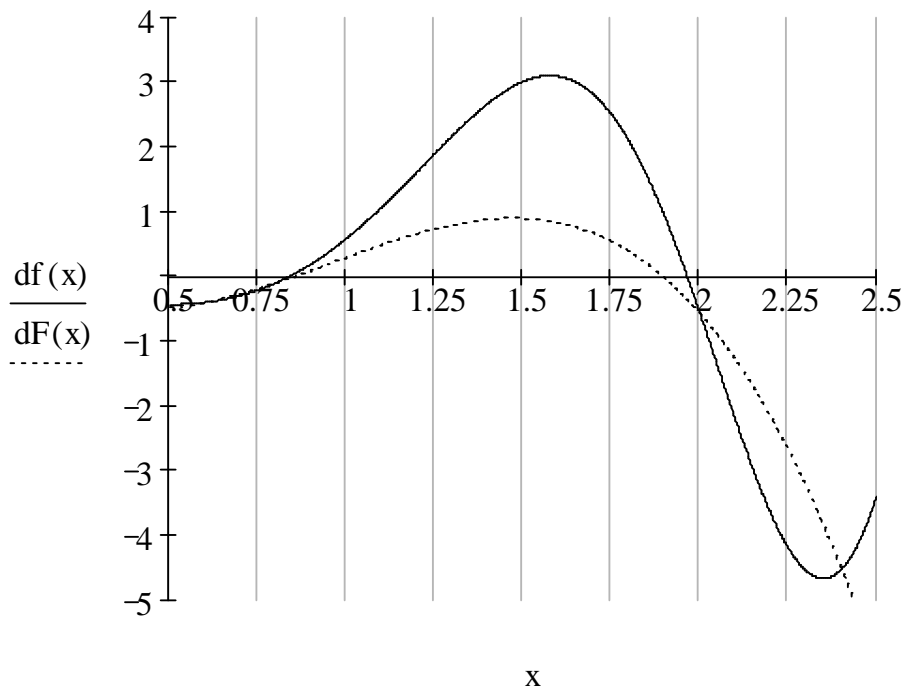
$$df(x) := 2 \cdot \cos(4 + x^2) \cdot x$$

$$X := \begin{pmatrix} 0.6 \\ 0.8 \\ 2 \\ 2.4 \end{pmatrix} \quad \begin{matrix} df(0.6) = -0.414 \\ df(0.8) = -0.116 \\ df(2) = -0.582 \\ df(2.4) = -4.533 \end{matrix} \quad Y := \begin{pmatrix} -0.414 \\ -0.116 \\ -0.582 \\ -4.533 \end{pmatrix}$$

$$vs := \text{cspline}(X, Y) \quad dF(x) := \text{interp}(vs, X, Y, x)$$

$$\text{Ot_Pogresh} := |df(1.6) - dF(1.6)| \cdot \frac{100}{f(1.6)}$$

$$\text{Ot_Pogresh} = 69.034$$



.5 -

4

,

(. . .1):

.1

	, %		
	18,274	107,074	2,27
	16,616	69,034	6,792

$$f(x) := 3 + \sin(4 + x^2)$$

$$X := \begin{pmatrix} 0.6 \\ 0.8 \\ 2 \\ 2.4 \end{pmatrix} \quad Y := \begin{pmatrix} 2.061 \\ 2.003 \\ 3.989 \\ 2.671 \end{pmatrix}$$

$$Fl(x) := \text{linterp}(X, Y, x)$$

$$vs := \text{cspline}(X, Y) \quad Fk(x) := \text{interp}(vs, X, Y, x)$$

$$\int_{0.5}^{2.4} f(x) dx = 5.418 \quad \int_{0.5}^{2.4} Fl(x) dx = 5.541 \quad \int_{0.5}^{2.4} Fk(x) dx = 5.786$$

$$\text{Ot_Pogresh_Fl} := |5.418 - 5.541| \cdot \frac{100}{5.418} \quad \text{Ot_Pogresh_Fl} = 2.27$$

$$\text{Ot_Pogresh_Fk} := |5.418 - 5.786| \cdot \frac{100}{5.418} \quad \text{Ot_Pogresh_Fk} = 6.792$$

.6 -

5 . , , 4 , -
, . , N·y0 -
18,274% **- 16,616%** . -
. -
4
1 **f₁(x)**, , -
; , .
2 **f₂(x)**, , -
; , .
3 **f₁(x), f₂(x)** -

$$f_1(x) = \frac{x}{1+x^4}; \quad f_2(x) = e^{\sqrt{1+\cos(x)}}.$$

1

l:

1.1

$$f(x) = \frac{x}{1+x^4}.$$

1.2

.

1.3

,

-2,

-

: = -2.

1.4

:

P_min := Min m ze (f, x).

1.5

: P = -0,76

-

f(x)

: f (-0,76) = -0,57.

1.6

: P_max := Max m ze (f, x).

1.7

P: = 0,76

-

f(x)

f (0,76) = 0,57.

MathCad

.7.

2

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,

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2

:

2.1

f (x): = .

2.2

.

,

,

,

, [-5; 2],

-

: = -2.

G ven

,

(

G ven

-

,

);

(

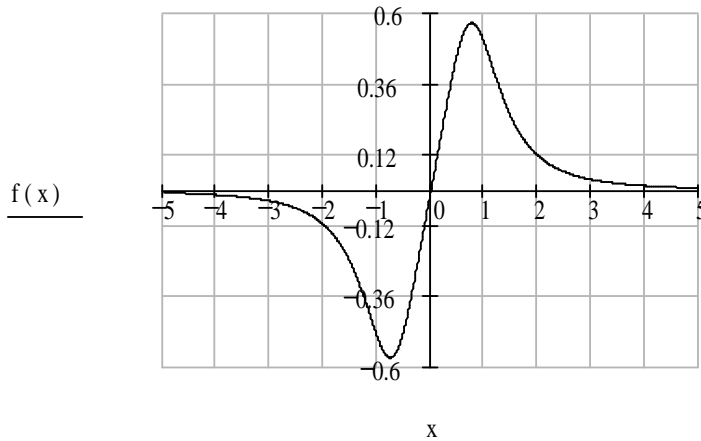
),

Boolean Toolbar /

-

: $x \geq -5 \leq 2.$

$$f(x) := \frac{x}{1 + x^4}$$



$$x := -2$$

$$P_{\min} := \text{minimize}(f, x)$$

$$P_{\min} = -0.76$$

$$P_{\max} := \text{maximize}(f, x)$$

$$P_{\max} = 0.76$$

$$f(P_{\min}) = -0.57$$

$$f(P_{\max}) = 0.57$$

.7 -

2.3

1.4-1.7

3

-

MathCad

.8.

3

3

:

3.1

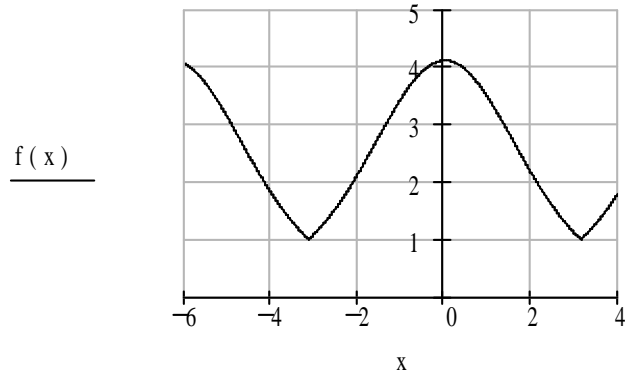
f1(x) f2(x).

3.2

MathCad

.9.

$$f(x) := e^{\sqrt{1 + \cos(x)}}$$



$$x := -2$$

given

$$x \leq 2 \quad x \geq -5$$

$$P_{\min} := \text{Minimize} \quad (f, x) \quad P_{\min} = -3.142$$

$$P_{\max} := \text{Maximize} \quad (f, x) \quad P_{\max} = 0$$

$$f(P_{\min}) = 1$$

$$f(P_{\max}) = 4.113$$

.8-

5

0,00001.

MathCad

1

$$\mathbf{x := 0, y := 2, TOL := 1 \cdot 10^{-5}}$$

2

G ven.

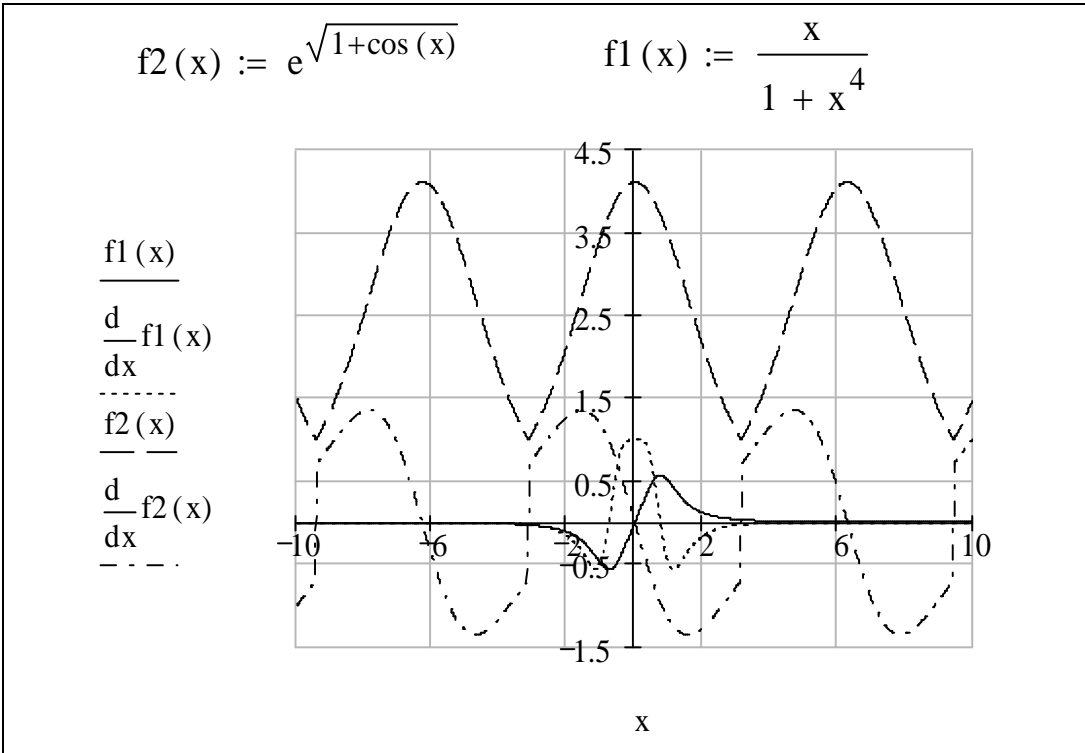
3

4

Find (x,)

=

$$\text{find}(x, y) = \begin{pmatrix} 0.331441665257368 \\ -0.662858829250469 \end{pmatrix}$$



.9-

, MathCad :

```

x := 0      y := 2

given

x7·√(4·x2 - y2) = 0

x - y + √(4·x2 - y2) = 1

find(x, y) = ( 0.331441665257368
              -0.662858829250469 )

x := 0.331441665257368

y := -0.662858829250469

x - y + √(4·x2 - y2) = 1

x7·√(4·x2 - y2) = 2.504 × 10-6

```

6

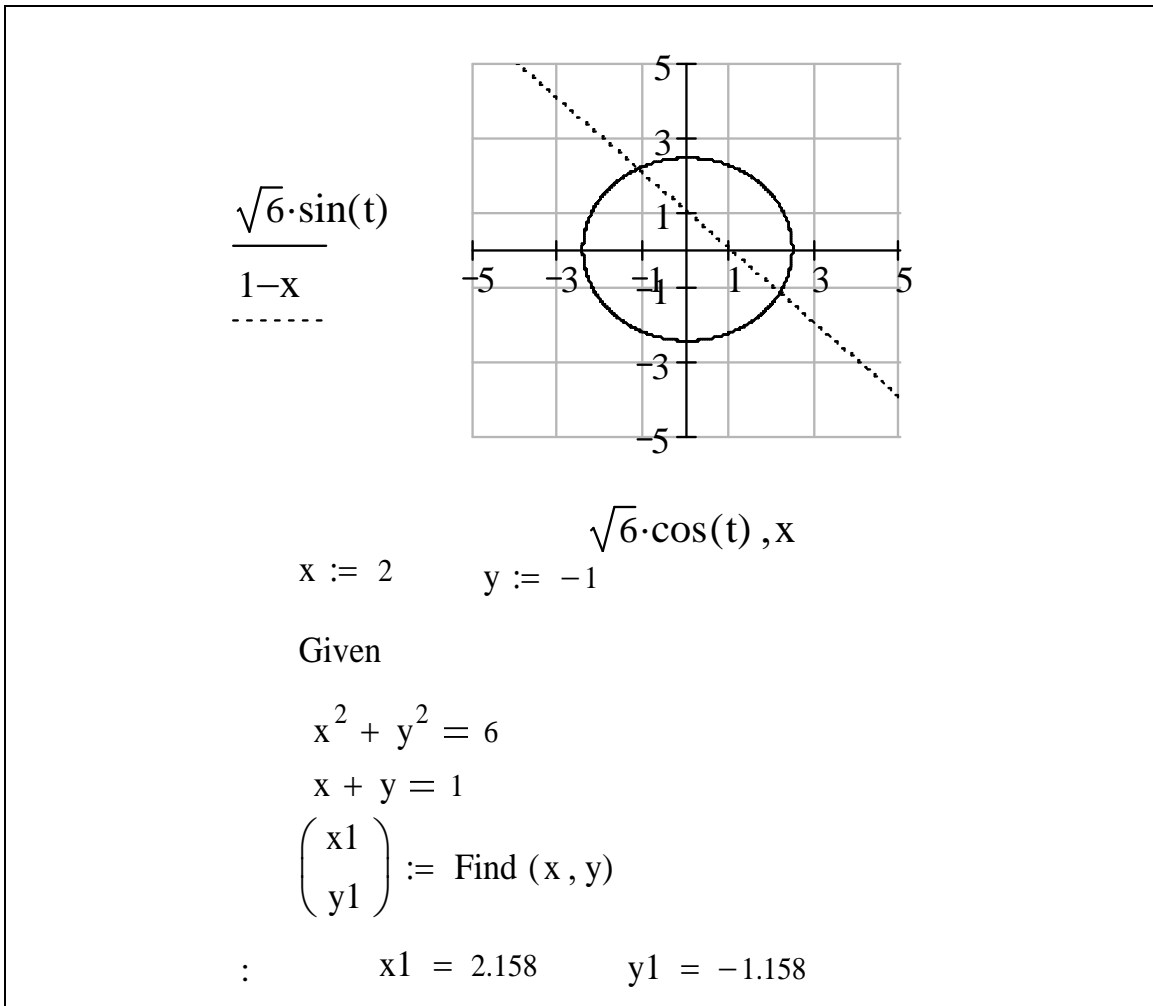
$$x^2 + y^2 = 6 \quad x + y = 1$$

().

$$y(t) = a \cdot \sin(t) \quad x(t) = a \cdot \cos(t), x-1 -$$

.10

$$x_1 = -1.158 \quad x_2 = 2.158.$$



.10 -

Find

7

f_1 , f_2
 $[x_n, x_k]$

.2

	f1	f2	(x _n)	y (x _k)	x _n	x _k
y + 9y	0	5(x + 2) ²	0	3	0	5

(rkf xed).

1

f1

1.1

$$: y := \begin{bmatrix} 0 \\ 3 \end{bmatrix}.$$

1.2

$$: \mathbf{1} := \mathbf{0},$$

2: = 5.

1.3

$$: \text{npoints} := 400.$$

1.4

$$: \mathbf{D}(\mathbf{x}, \mathbf{y}) := \begin{bmatrix} y_1 \\ -9 \cdot y_0 \end{bmatrix}.$$

1.5

$$\mathbf{Z} := \text{rkf xed} (y, x_1, x_2, \text{npoints}, \mathbf{D}).$$

$\mathbf{Z}^{<0>}$,

$-\mathbf{Z}^{<1>}$.

2

f2

2.1

$$\mathbf{D}(\mathbf{x}, \mathbf{y}) := \begin{bmatrix} y_1 \\ 5 \cdot (\mathbf{x} + 2)^2 - 9 \cdot y_0 \end{bmatrix}.$$

2.2

$$: \mathbf{Z} := \text{rkf xed} (y, x_1, x_2, \text{npoints}, \mathbf{D}).$$

2.3

$\mathbf{Z}^{<0>}$,

$-\mathbf{Z}^{<1>}$.

MathCad

.11.

$$y := \begin{pmatrix} 0 \\ 3 \end{pmatrix} \quad x1 := 0 \quad x2 := 5 \quad npoints := 400$$

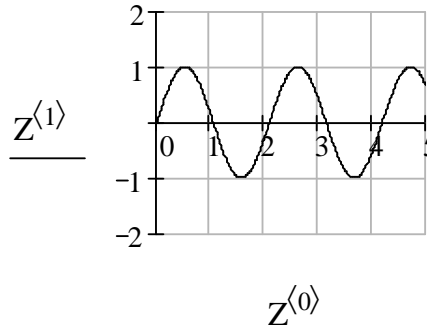
$$D(x, y) := \begin{pmatrix} y_1 \\ -9 \cdot y_0 \end{pmatrix} \quad Z := \text{rkfixed}(y, x1, x2, npoints, D)$$

$$Z^{(0)} =$$

	0
0	0
1	0.013
2	0.025
3	0.038
4	0.05
5	0.063
6	0.075
7	0.088
8	0.1
9	0.113
10	0.125
11	0.137
12	0.15
13	0.163
14	0.175
15	0.188

$$Z^{(1)} =$$

	0
0	0
1	0.037
2	0.075
3	0.112
4	0.149
5	0.186
6	0.223
7	0.259
8	0.296
9	0.331
10	0.366
11	0.401
12	0.435
13	0.468
14	0.501
15	0.533



$$D(x, y) := \begin{bmatrix} y_1 \\ -9 \cdot y_0 + 5 \cdot (x + 2)^2 \end{bmatrix} \quad Z := \text{rkfixed}(y, x1, x2, npoints, D)$$

$$Z^{(0)} =$$

	0
0	0
1	0.013
2	0.025
3	0.038
4	0.05
5	0.063
6	0.075
7	0.088
8	0.1
9	0.113
10	0.125
11	0.137
12	0.15
13	0.163
14	0.175
15	0.188

$$Z^{(1)} =$$

	0
0	0
1	0.039
2	0.081
3	0.126
4	0.175
5	0.226
6	0.281
7	0.338
8	0.398
9	0.461
10	0.527
11	0.596
12	0.668
13	0.742
14	0.819
15	0.898

.11 - ,

y

$$y := \begin{pmatrix} 9 \\ 16 \\ 25 \\ 36 \\ 49 \end{pmatrix} \quad h := 0.25$$

$$m := \text{length}(y) - 1 \\ m = 4$$

1. :

$$i := 0..m-1 \quad I := \left(\frac{h}{2}\right) \cdot \sum_i (y_i + y_{i+1}) \quad I = 26.5$$

2. ():

$$i := 1,3..m-1 \quad j := 2,4..m-2 \\ I := \left(\frac{h}{3}\right) \cdot \left(y_0 + y_m + 4 \cdot \sum_i y_i + 2 \cdot \sum_j y_j \right) \quad I = 26.333$$

3. ()

$$i := 0..m \quad t_i := i \cdot h \\ I := \int_0^{m \cdot h} \text{linterp}(t, y, x) \, dx \quad I = 26.5$$

4. () () :

$$s := \text{cspline}(t, y)$$

$$I := \int_0^{m \cdot h} \text{interp}(s, t, y, x) \, dx \quad I = 26.5$$

5. ():

$$I := h \cdot \int_3^7 x^2 \, dx \quad I = 26.333$$

1

: (. .1)

.1

	$y(x) =$		$y(x) =$
1	$3 - \cos(x^2)$	14	$\text{Ln}(4 - \cos x)$
2	$e^{\sin(x+4)}$	15	$2,5 + \cos(x^2)$
3	$e^{\cos 2x}$	16	$\sin 2x + \cos^2 2x$
4	$2 + \ln(3 + \sin x)$	17	$e^{\cos(2+x)}$
5	$3 + \sin(4 + x^2)$	18	$2 - \sin(2x)$
6	$\ln(5 - \cos x)$	19	$e^{(1 + \sin \frac{x}{2})}$
7	$e^{\sin(2x)}$	20	$\ln(3 + \sin \frac{x}{2})$
8	$1,5 + \cos(1 + 2x)$	21	$e^{\sin \frac{x}{2}}$
9	$\ln(4 + \sin(2x))$	22	$\ln(3 - \cos x^2)$
10	$2 + \cos(x)$	23	$2 - \sin \frac{x^2}{2}$
11	$3 \sin(e^x)$	24	$\sin 3x + \cos(x + 5)$
12	$1,1 + \cos(e^x)$	25	$2 + \sin x$
13	$2 + \sin(x^2)$	26	$\sin(2x + 2) - 1$

2

1 (. .2) ,
 2 (. .2).
 3 , 10-5
 (. .3).

.2

1	2	3
1	$e^x + x = 0$	$x^2 - 12x - 4 = 0$
2	$\sin x - \frac{1}{x} = 0$	$x^3 - 24x + 11 = 0$
3	$\cos x - \frac{1}{x+2} = 0$	$x^3 + 2x - 7 = 0$
4	$\cos x + \frac{1}{x+2} = 0$	$x^3 - 21x + 7 = 0$
5	$x = e^{-x+20}$	$x^3 - 5x + 1 = 0$
6	$\cos x^2 - x = 0$	$x^3 - 12x + 5 = 0$
7	$e^{-x} - 2x = 0$	$x^3 + 3x^2 - 4x - 1 = 0$
8	$\cos x - \frac{1}{x^2 + 3} = 0.5$	$x^3 - 9x^2 + 20x - 11 = 0$
9	$\cos x - \frac{1}{x^2 + 3} = 0,5$	$x^3 - 12x + 5 = 0$
10	$5 \cdot \cos x - x = \cos^2 x$	$x^3 + 6x^2 + 6x - 7 = 0$
11	$x^2 - \cos x^3 = 0$	$x^3 - 3x^2 - x + 2 = 0$
12	$e^x + 2 \sin x = 0$	$x^3 - 10x^2 + 4x + 9 = 0$
13	$\sin x - \frac{1}{x-5} = 3x$	$x^4 + x - 1 = 0$
14	$\cos x - \frac{1}{x} = 0$	$x^3 - 3x^2 - 4x + 1 = 0$
15	$5 \cos x - x = \cos x$	$x^3 - 34x^2 + 4x + 1 = 0$
16	$\sqrt[4]{2 x } + x^3 = 0$	$x^3 - 27x - 17 = 0$
17	$\ln(x) + \sqrt{x} = 0$	$x^4 - 2x^3 + 2x^2 - 2x + 1 = 0$

.2

1	2	3
18	$3^x - 21 + 8x^3 = 9x$	$x^4 - 3x^3 + 3x^2 - 3x + 2 = 0$
19	$4 - x - \frac{4}{x^2} = 0$	$x^4 - 3x^3 + 5x^2 - 3x + 8 = 0$
20	$2\sqrt{x} - x - 0,5 = 0$	$x^4 - 4x^3 + 8x^2 - 4x + 16 = 0$
21	$x - 4\sqrt{x} + 3 = 0$	$x^4 - 4x^3 + 4x^2 - 4x + 3 = 0$
22	$2x^2 + \frac{108}{x^2} - 59 = 0$	$x^4 - 4x^3 + 12x^2 - 4x + 27 = 0$
23	$x^2 + \frac{16}{x} - 16 = 0$	$x^4 - 6x^3 + 18x^2 - 6x + 81 = 0$
24	$2\sqrt{x} - x - 0,5 = 0$	$x^4 - 5x^3 + 10x^2 - 5x + 24 = 0$
25	$\frac{10x}{x^2 + 1} = 3$	$x^4 - 5x^3 + 15x^2 - 5x + 54 = 0$

.3

1	2	1	2
1	$\begin{cases} x^2 - y^3 = 2 \\ x^2 + y = 0 \end{cases}$	14	$\begin{cases} x^2 + y^3 = 0 \\ x^2 - y = 0 \end{cases}$
2	$\begin{cases} x^2 + \cos x = 12 \\ x^2 + y = 0 \end{cases}$	15	$\begin{cases} x^2 - \cos x - 2 = 9 \\ x^2 + y^3 = 9 \end{cases}$
3	$\begin{cases} y^2 - \operatorname{tg} x^2 = 2 \\ x + y^3 = 9 \end{cases}$	16	$\begin{cases} x^2 - y^3 = 2 \\ x^2 + y = 0 \end{cases}$
4	$\begin{cases} x^2 + y^3 = 0 \\ x^2 - y = 0 \end{cases}$	17	$\begin{cases} x^2 + \cos x = 12 \\ x^2 + y = 0 \end{cases}$
5	$\begin{cases} 1,5y = 1,3 \ln(x+2) \\ \frac{1,3}{3^{2x}} = y \end{cases}$	18	$\begin{cases} 1,5y = 1,3 \ln(x+2) \\ 2y = 1,3(x-1,3)^3 \end{cases}$
6	$\begin{cases} 1,5y = 1,3 \ln(x+2) \\ y = 2 \operatorname{tg}(x+1,3) \end{cases}$	19	$\begin{cases} y = \frac{1,3}{3^{2x}} \\ 2y = 1,3(x-1,3)^3 \end{cases}$

1	2	1	2
7	$\begin{cases} y = \frac{1,3}{3^{2x}} \\ y = 2 \operatorname{arctg} (x+1,3) \end{cases}$	20	$\begin{cases} 2y = 1,3(x-1,3)^3 \\ y = 2 \operatorname{tg} (x+1,3) \end{cases}$
8	$\begin{cases} x^2 + y^2 = 4 \\ 3x+1 = y \end{cases}$	21	$\begin{cases} x^2 + y^2 = 16 \\ y - 3x - 1 = 0 \end{cases}$
9	$\begin{cases} x^3 + y = 9 \\ y = 3x + 5 \end{cases}$	22	$\begin{cases} x^2 + y^2 = 16 \\ y = 3x + 5 \end{cases}$
10	$\begin{cases} x^3 + y = 9 \\ y = 3,5x - 5 \end{cases}$	23	$\begin{cases} x^2 + y^3 = 16 \\ y = 3x + 5 \end{cases}$
11	$\begin{cases} x^3 - y^{-x} = 9 \\ y - 3,5x + 5 = 0 \end{cases}$	24	$\begin{cases} x^3 + y = 16 \\ y - 3x = 5 \end{cases}$
12	$\begin{cases} x^2 - y^{-x} = 1 \\ y = 3,5x - 5 \end{cases}$	25	$\begin{cases} x^2 + \cos x = 12 \\ x^2 + y = 0 \end{cases}$
13	$\begin{cases} x^2 + y^{-x} = \cos x \\ y = 3,5x - 5 \end{cases}$	26	$\begin{cases} x^2 + \cos x = 12 \\ x^2 + y = 0 \end{cases}$

3 ,

:

1 (. .4) -

$$A \cdot X = B.$$

2 $\Delta = \det A$

3 :

$$) : X = A^{-1} \cdot B;$$

)

Isolve (A, B).

4 , .

1	2
1	$\begin{cases} 0,005x_1 + 0,004x_2 + 0,150x_3 = 0,057 \\ -0,090x_1 - 0,033x_2 + 0,0067x_3 - 0,098x_4 = -0,098 \\ 0,150x_1 + 0,033x_2 + 0,050x_3 + 0x_4 = 0,183 \\ 2,857x_1 + 0,100x_2 - 0,300x_3 + 0,025x_4 = -0,041 \end{cases}$
2	$\begin{cases} 0,010x_1 + 0,008x_2 + 0,200x_3 + 0,050x_4 = 0,186 \\ -0,080x_1 + 0,013x_3 - 0,050x_4 = -0,126 \\ 0,250x_1 + 0,067x_2 + 0,067x_3 + 0,069x_4 = 0,646 \\ 0,057x_1 + 0,150x_2 - 0,267x_3 + 0,050x_4 = 0,0086 \end{cases}$
3	$\begin{cases} 0,015x_1 + 0,012x_2 + 0,250x_3 + 0,100x_4 = 0,388 \\ -0,070x_1 - 0,033x_2 + 0,020x_3 - 0,075x_4 = -0,084 \\ 0,350x_1 + 0,100x_2 + 0,075x_3 + 0,110x_4 = 1,357 \\ 0,0086x_1 + 0,200x_2 - 0,233x_3 + 0,075x_4 = 0,149 \end{cases}$
4	$\begin{cases} 0,020x_1 + 0,016x_2 + 0,300x_3 + 0,150x_4 = 0,662 \\ -0,060x_1 + 0,067x_2 + 0,027x_3 - 0,100x_4 = 0,029 \\ 0,450x_1 + 0,133x_2 + 0,080x_3 + 0,139x_4 = 2,312 \\ 0,011x_1 + 0,250x_2 - 0,200x_3 + 0,100x_4 = 0,379 \end{cases}$
6	$\begin{cases} 0,030x_1 + 0,024x_2 + 0,400x_3 + 0,250x_4 = 1,427 \\ -0,040x_1 + 0,133x_2 + 0,040x_3 + 0,150x_4 = 0,465 \\ 0,650x_1 + 0,200x_2 + 0,086x_3 + 0,179x_4 = 4,940 \\ 0,017x_1 + 0,350x_2 - 0,133x_3 + 0,150x_4 = 1,111 \end{cases}$
7	$\begin{cases} 0,035x_1 + 0,028x_2 + 0,450x_3 + 0,300x_4 = 1,918 \\ -0,030x_1 + 0,167x_2 + 0,047x_3 + 0,175x_4 = 0,788 \\ 0,750x_1 + 0,233x_2 + 0,088x_3 + 0,195x_4 = 6,611 \\ 0,020x_1 + 0,400x_2 - 0,100x_3 + 0,175x_4 = 1,613 \end{cases}$
8	$\begin{cases} 0,040x_1 + 0,032x_2 + 0,500x_3 + 0,350x_4 = 2,481 \\ -0,020x_1 + 0,200x_2 + 0,053x_3 + 0,200x_4 = 1,182 \\ 0,850x_1 + 0,267x_2 + 0,089x_3 + 0,208x_4 = 8,520 \\ 0,023x_1 + 0,450x_2 - 0,067x_3 + 0,200x_4 = 2,205 \end{cases}$

9	$\begin{cases} 0,045x_1 + 0,036x_2 + 0,550x_3 + 0,400x_4 = 3,117 \\ -0,010x_1 + 0,233x_2 + 0,060x_3 + 0,225x_4 = 1,646 \\ 0,950x_1 + 0,300x_2 + 0,090x_3 + 0,220x_4 = 10,664 \\ 0,026x_1 + 0,500x_2 - 0,033x_3 + 0,225x_4 = 2,888 \end{cases}$
10	$\begin{cases} 0,050x_1 + 0,040x_2 + 0,600x_3 + 0,450x_4 = 3,825 \\ 0,267x_2 + 0,067x_3 + 0,250x_4 = 2,181 \\ 1,050x_1 + 0,333x_2 + 0,091x_3 + 0,230x_4 = 13,045 \\ 0,029x_1 + 0,550x_2 + 0,250x_4 = 3,661 \end{cases}$
11	$\begin{cases} 0,055x_1 + 0,044x_2 + 0,065x_3 + 0,500x_4 = 4,605 \\ 0,010x_1 + 0,300x_2 + 0,073x_3 + 0,275x_4 = 2,785 \\ 1,150x_1 + 0,367x_2 + 0,092x_3 + 0,240x_4 = 15,662 \\ 0,031x_1 + 0,600x_2 + 0,033x_3 + 0,750x_4 = 4,524 \end{cases}$
12	$\begin{cases} 0,060x_1 + 0,048x_2 + 0,700x_3 + 0,550x_4 = 5,458 \\ 0,020x_1 + 0,333x_2 + 0,080x_3 + 0,300x_4 = 3,460 \\ 1,250x_1 + 0,400x_2 + 0,092x_3 + 0,248x_4 = 18,515 \\ 0,034x_1 + 0,650x_2 + 0,067x_3 + 0,300x_4 = 5,478 \end{cases}$
13	$\begin{cases} 0,065x_1 + 0,052x_2 + 0,750x_3 + 0,600x_4 = 6,383 \\ 0,030x_1 + 0,367x_2 + 0,087x_3 + 0,325x_4 = 4,205 \\ 1,350x_1 + 0,433x_2 + 0,093x_3 + 0,256x_4 = 21,603 \\ 0,037x_1 + 0,700x_2 + 0,100x_3 + 0,325x_4 = 6,522 \end{cases}$
14	$\begin{cases} 0,070x_1 + 0,056x_2 + 0,800x_3 + 0,650x_4 = 7,380 \\ 0,040x_1 + 0,400x_2 + 0,093x_3 + 0,350x_4 = 5,021 \\ 1,450x_1 + 0,467x_2 + 0,093x_3 + 0,264x_4 = 24,926 \\ 0,040x_1 + 0,750x_2 + 0,133x_3 + 0,350x_4 = 7,657 \end{cases}$
15	$\begin{cases} 0,075x_1 + 0,060x_2 + 0,850x_3 + 0,700x_4 = 8,450 \\ 0,050x_1 + 0,433x_2 + 0,100x_3 + 0,375x_4 = 5,906 \\ 1,550x_1 + 0,500x_2 + 0,094x_3 + 0,248x_4 = 28,484 \\ 0,043x_1 + 0,800x_2 + 0,167x_3 + 0,375x_4 = 8,882 \end{cases}$

16	$\begin{cases} 0,080x_1 + 0,064x_2 + 0,900x_3 + 0,750x_4 = 9,592 \\ 0,060x_1 + 0,467x_2 + 0,107x_3 + 0,400x_4 = 6,862 \\ 1,650x_1 + 0,533x_2 + 0,094x_3 + 0,277x_4 = 32,278 \\ 0,046x_1 + 0,850x_2 + 0,200x_3 + 0,400x_4 = 10,198 \end{cases}$
17	$\begin{cases} 0,085x_1 + 0,068x_2 + 0,950x_3 + 0,800x_4 = 10,806 \\ 0,070x_1 + 0,500x_2 + 0,113x_3 + 0,425x_4 = 7,888 \\ 1,750x_1 + 0,567x_2 + 0,094x_3 + 0,283x_4 = 36,306 \\ 0,049x_1 + 0,900x_2 + 0,233x_3 + 0,425x_4 = 11,604 \end{cases}$
18	$\begin{cases} 0,090x_1 + 0,072x_2 + 1,000x_3 + 0,850x_4 = 12,093 \\ 0,080x_1 + 0,533x_2 + 0,120x_3 + 0,450x_4 = 8,985 \\ 1,850x_1 + 0,600x_2 + 0,095x_3 + 0,289x_4 = 40,569 \\ 0,051x_1 + 0,950x_2 + 0,267x_3 + 0,450x_4 = 13,101 \end{cases}$
19	$\begin{cases} 0,095x_1 + 0,076x_2 + 1,050x_3 + 0,900x_4 = 13,452 \\ 0,090x_1 + 0,567x_2 + 0,127x_3 + 0,475x_4 = 10,152 \\ 1,950x_1 + 0,633x_2 + 0,095x_3 + 0,294x_4 = 45,067 \\ 0,054x_1 + 1,000x_2 + 0,300x_3 + 0,475x_4 = 14,688 \end{cases}$
20	$\begin{cases} 0,100x_1 + 0,080x_2 + 1,100x_3 + 0,950x_4 = 14,883 \\ 0,100x_1 + 0,600x_2 + 0,133x_3 + 0,500x_4 = 11,389 \\ 2,050x_1 + 0,667x_2 + 0,095x_3 + 0,300x_4 = 49,799 \\ 0,057x_1 + 1,050x_2 + 0,333x_3 + 0,500x_4 = 16,365 \end{cases}$

4

:

- 1 $f(x)$ (. .5) x .
- 2 () -
- n** .
- 3 $f(x)$ $[a, b]$ (. .6).
- 4 () .

.5

	$f(x) =$	$x =$	$n =$		$f(x) =$	$x =$	$n =$
1	e^{-x^2}	2	3	9	$\frac{x}{x^2-1}$	2	4
2	$\sin 2x$	5	2	10	$x e^{5x}$	1	3
3	e^{3x}	8	4	11	$\ln 3x$	3	4
4	\sqrt{x}	4	2	12	$\sqrt{2x+3}$	4	3
5	$\frac{x^2}{x-1}$	7	6	13	$\frac{2x+3}{4x+7}$	5	3
6	$x^2 \sin 2x$	3	2	14	$\sin^2 x$	6	3
7	$x^3 \cos 5x$	1	3	15	$\cos^2 x$	7	3
8	$\frac{x-1}{x+1}$	9	4	16	$\cos^3 x$	8	3

.6

	$f(x)$	a	b		$f(x)$	a	b
1	2	3	4	1	2	3	4
1	$\frac{x+1}{\sqrt{x}}$	1	6	10	$\sqrt{1+\sin 2x}$	0	4
2	$(x^4+1)x^3$	2	5	11	$(2x-3)^{10}$	2	6
3	$\frac{x^2}{1-x^2}$	2	5	12	$\frac{1}{\sqrt{2-5x}}$	1	3
4	$t g^2 x$	-1	1	13	$\frac{1}{2+3x^2}$	-1	1
5	$\frac{2x+3}{3x+2}$	0	4	14	$\frac{1}{\sqrt{3x^2-2}}$	2	3
6	$\sqrt{1-\sin 2x}$	4	6	15	$\frac{1}{\sin^2(2x+\frac{\pi}{4})}$	1,5	2,7
7	$(3-x^2)^3$	2	3	16	$\frac{1}{1+\cos x}$	1	3
8	$(1-\frac{1}{x^2})\sqrt{x\sqrt{x}}$	1	5	17	$\frac{1}{1+\sin x}$	1	3
9	$\frac{\sqrt{x^4+x^{-4}+2}}{x^3}$	2	3	18	$\frac{1}{\sqrt{1+x^2}}$	2	4

.6

1	2	3	4	1	2	3	4
19	$\frac{x^2+3}{x^2-1}$	2	3	23	$\frac{x^3}{x^8-2}$	7	8
20	$\frac{2^{x+1}-5^{x-1}}{10^x}$	-2	-1	24	$\frac{1}{x\sqrt{x^2+1}}$	4	5
21	$\frac{\sqrt{1+x^2}+\sqrt{1-x^2}}{\sqrt{1-x^4}}$	-3	-1	25	$\frac{1}{x\sqrt{x^2-1}}$	2	3
22	$(2^x+3^x)^2$	1	2	26	tgx	-1	1

5

:

1

(. .7).

2

(. .8).

.7

1	$3\sqrt[3]{(x+4)^2-2x-8}$	6	$3\sqrt[3]{(x-1)x}$
2	$1-\sqrt[3]{x^2-2x}$	7	$\frac{6\sqrt[3]{6x^2}}{(x+2)^2+8}$
3	$12\sqrt[3]{(x+2)^2-8x-16}$	8	$2x-2-3\sqrt[3]{(x-1)^2}$
4	$\frac{12\sqrt[3]{6(x-2)^2}}{x^2+8}$	9	$2+\sqrt[3]{8x(x+2)}$
5	$8x-16-12\sqrt[3]{(x+4)^2}$	10	$\frac{3\sqrt[3]{6(x-4)^2}}{x^2-4x+12}$

.7

1	2	1	2
11	$\frac{12\sqrt[3]{6(x-1)^2}}{(x+1)^2+8}$	12	$3\sqrt[3]{(x-2)^2}-2x+4$
12	$9\sqrt[3]{(x+1)^2}-6x-6$	13	$-\frac{3\sqrt[3]{6(x+1)^2}}{(x+3)^2+8}$
13	$1-\sqrt[3]{(x-2)^2-1}$	14	$\sqrt[3]{(x+2)^2-1}$
14	$\sqrt[3]{(x+4)x}$	15	$\sqrt[3]{(x+4)(x-4)}$
11	$\frac{6\sqrt[3]{6(x-3)^2}}{(x-1)^2+8}$	16	$\frac{3\sqrt[3]{6(x-5)^2}}{(x-3)^2+8}$

.8

1	2	3	1	2	3
1	$\sqrt[3]{2(x-2)^2(8-x)}-1$	[0; 6]	11	$2-x-\frac{4}{(x+2)^2}$	[-1; 2]
2	$4-x-\frac{4}{x^2}$	[1; 4]	12	$\sqrt[3]{2x^2(x-3)}$	[-1; 6]
3	$x^2+\frac{16}{x}-16$	[1; 4]	13	$\frac{2(-x^2+7x-7)}{x^2-2x+2}-1$	[1; 4]
4	$2\sqrt{x}-x-0,5$	[0; 4]	15	$1-\sqrt[3]{2(x-2)^2(5-x)}$	[1; 5]
5	$1+\sqrt[3]{2(x-1)^2(x-7)}$	[-1; 5]	16	$\frac{4x}{x^2+4}$	[-4; 2]
6	$x-4\sqrt{x}+3$	[1; 9]	17	$8+\frac{8}{x}-\frac{x^2}{2}$	[-4; -1]
7	$\frac{10x}{x^2+1}-3$	[0; 3]	18	$1+\sqrt[3]{2x^2(x-6)}$	[-2; 4]
8	$-2+\sqrt[3]{2(x+1)^2(5-x)}$	[-3; 3]	19	$\frac{2x(2x+3)}{x^2+4x+5}$	[-2; 1]
9	$2x^2+\frac{108}{x^2}-59$	[2; 4]	20	$-\frac{2(x^2+3)}{x^2+2x+5}+2$	[-5; -2,8]
10	$\frac{2(x^2+3)}{x^2-2x+5}-1$	[-3; 3]	14	$x-4\sqrt{x+2}+5,5$	[-1; 7]

6

1
 .9).
 2
 x_0 .

f(x) (. .10) n -

.9

1	2	3	4	5	6	7
1	X	0,8	0,9	1	1,5	2
	Y	2,5	2,22	2	1,333	1
2	X	0,8	0,9	1	1,5	2
	Y	-0,223	-0,105	0	0,405	0,693
3	X	0,8	0,9	1	1,5	2
	Y	0,928	0,965	1	1,145	1,26
4	X	1	1,5	2	2,5	3
	Y	0,707	0,924	1	0,924	0,707
5	X	4	4,5	5	5,5	6
	Y	2	1,2	0,833	0,629	0,5
6	X	1	1,5	2	2,5	3
	Y	0,25	0,333	0,4	0,455	0,5
7	X	0,8	0,9	1	1,5	2
	Y	0,527	0,445	0,368	0,105	0,018

1	2	3	4	5	6	7
8	X	0,8	0,9	1	1,5	2
	Y	1,17	1,216	1,26	1,442	1,587
9	X	0,8	0,9	2	2,5	3
	Y	3,75	3,333	3	2	1,5
10	X	0,8	0,9	1	1,5	2
	Y	0,247	0,482	0,693	1,504	2,079
11	X	1	1,5	2	2,5	3
	Y	0,368	0,223	0,135	0,082	0,05
12	X	0,8	0,9	1	1,5	2
	Y	-0,14	-0,07	0	0,27	0,462
13	X	1,2	1,5	2	2,2	2,3
	Y	0,667	1	2	2,75	3,286
14	X	0	0,5	1	1,5	2
	Y	1	1,125	2	4,375	9
15	X	1	1,5	2	2,5	3
	Y	0,707	0,583	1	0,383	0,77
16	X	0,5	0,7	0,8	1,3	1,8
	Y	-3	-2,44	-2,2	-1,076	0,053
17	X	0	0,5	1	1,5	2
	Y	-0,736	-0,963	-1	-1,047	-1,437

.9

1	2	3	4	5	6	7
18	X	1,2	1,7	2	2,5	3
	Y	-4,64	-4,017	-4	-3,953	-3,693
19	X	0,1	0,5	1	1,5	2
	Y	-2,262	-1,097	-1	-0,881	-0,266
20	X	0	0,5	1	1,5	2
	Y	0,708	0,98	1	0,98	0,708
21	X	0	0,5	1	1,5	2
	Y	-0,736	-1,463	-3	-5,547	-9,437
22	X	-0,9	-0,5	0	1	1,5
	Y	-0,995	0,864	1	1,386	2,083
23	X	0,5	1	2	3	3,5
	Y	-1,255	-0,292	0	-0,292	-1,255
24	X	-3	-2,5	-2	-1,5	-1
	Y	14,987	11,228	7,963	5,19	2,9

.10

	f(x)	x₀	n		f(x)	x₀	n
1	2	3	4	1	2	3	4
1	$\frac{2}{x}$	1	3	5	$\frac{x}{3-x}$	2	3
2	$\ln x$	1	4	6	$x^3 + 1$	1	4
3	$\sqrt[3]{x}$	1	3	7	$\cos \frac{\pi}{4}x$	2	3
4	$\sin \frac{\pi}{4}x$	2	4	8	$(x - \frac{\pi}{4}) \sin x$	$\frac{\pi}{4}$	4

1	2	3	4	1	2	3	4
9	$\frac{x}{x^2 - 5x + 6}$	5	3	17	$x^2 - 2e^{x-1}$	1	5
10	$\frac{x}{3+x}$	2	4	18	$x^2 - 4x - (x-2)\ln(x-1)$	2	4
11	e^{-x^2}	1	3	19	$x^2 - 2x - (x-1)\ln x$	1	4
12	$\sqrt[3]{2x}$	1	4	20	$\sin^2(x-1) - x^2 + 2x$	1	5
13	$\frac{3}{x}$	2	3	21	$-x^2 - 2e^{x-1}$	1	5
14	$\ln(2x^2)$	1	4	22	$x^2 - 2x + 1 + 2\ln(x+1)$	0	4
15	e^{-x}	2	3	23	$\sin^2(x-2) - x^2 + 4x - 4$	2	5
16	$\cos^2(x-1) - x^2$	1	4	24	$x^2 - 2x - 2e^{x-2}$	-2	5

7

:

.11

[xn, xk]

f1,

f2.

.11

		f1	f2	y(0)	y'(0)	xn	xk
1	2	3	4	5	6	7	8
1	$y'' + \pi y$	0	$1 - x^2 \sin x$	1	0	1	6
2	$y'' + 6y' + 8y$	0	$6x^2 + 3 \cos x$	-1	0	-1	3
3	$y'' + \frac{y}{4}$	0	$(1 - 2x)e^x$	0	1	0	3
4	$y'' + 3y'$	0	$e^x \cos 2x$	0	-1	0	5
5	$y'' + 9y$	0	$5(x+2)^2$	0	3	0	5

1	2	3	4	5	6	7	8
6	$y'' - 3y' + 2y$	0	$(3x + 7)e^{2x}$	0	-3	0	2
7	$y'' + 4y$	0	$x^2 + x - 1$	3	0	3	10
8	$y'' + 9y$	0	$\cos 4x + 1$	-3	0	-3	3
9	$y'' + 3y' + 2y$	0	$(2x + 5)e^{2x}$	2	0	-2	2
10	$y'' - 6y' + 8y$	0	$4x^2 \sin x$	-2	0	-2	-1
11	$y'' - y'$	0	$(16 - 2x)e^{-x}$	0	2	3	6
12	$y'' + 4y$	0	$5x^2 - 1$	0	-2	0	9
13	$y'' - 9y' + 18y$	0	$4(1 - x)e^{-x}$	4	0	4	5
14	$y'' + 4y$	0	$x - x^2 + 2 \cos x$	-4	0	-4	4
15	$y'' + 6y$	0	$e^{x+2} \cos x$	0	4	0	5
16	$y'' + \pi^2 y$	0	$3x^2 + 2x$	1	0	1	6
17	$y'' - 3y' + 2y$	0	$(12 - 16x)e^x$	-1	0	2	3
18	$y'' + y'$	0	$3x^2 + 2\sqrt{x} + 1$	0	1	0	5
19	$y'' + 5y$	0	$(20x + 14)e^{2x}$	0	-1	0	1
20	$y'' + 16y$	0	$x \cos x + 2$	0	3	0	6
21	$y'' + y$	0	$1 + \cos^3 x$	0	-3	0	7
22	$y'' - 3y'$	0	$(20x + 14)e^{2x}$	3	0	0	1
23	$y'' - 6y' + 8y$	0	$12x^2 - 6x$	-3	0	0.5	1,5
24	$y'' - 3y' + 2y$	0	$49 - 24x^2$	2	0	3	4
25	$y'' + y$	0	$3x^2 + x - 4$	-2	0	2	7

8

- :
- 1) fio_2.dat);
- 2) lab2.mcd
- fio_2.mcd;
- 3) mean, R=xmin-xmax,
Sk, Ex.
- 4) 10.
- 5)
- 6) 10%
- %.

I

1.67	2.41	0.79	1.41	2.50	2.29	2.58	1.32
3.75	1.94	0.95	3.48	2.39	1.17	1.92	1.04
2.13	1.58	2.18	2.30	3.03	1.50	2.53	1.91
1.31	3.62	1.49	1.98	2.14	3.35	2.89	2.51
2.31	2.34	1.00	2.03	0.64	2.67	0.09	1.78
3.24	1.91	1.20	1.61	2.35	1.73	2.93	2.32
2.84	1.29	2.28	2.54	1.85	2.40	2.22	2.90
2.37	2.68	2.00	2.70	2.33	2.86	0.36	1.98
2.53	0.80	2.89	0.73	1.01	1.85	2.05	1.16
1.76	2.78	2.43	1.85	1.21	1.53	1.54	2.43

P (0.93 < X < 1.52) = ?

2

2.46	1.70	2.44	0.82	1.50	2.53	2.32	2.61
1.35	3.78	1.97	0.98	3.51	2.42	1.20	1.95
1.07	2.16	1.61	2.21	2.33	3.06	1.53	2.56
1.94	1.34	3.63	1.52	2.01	2.17	3.38	2.92
2.54	2.34	2.37	1.03	2.06	0.67	2.70	1.12
1.81	3.27	1.94	1.23	1.64	2.38	1.76	2.96
2.35	2.87	1.32	2.31	2.57	1.88	2.43	1.88
2.93	2.40	2.71	2.03	2.76	2.36	2.89	0.39
2.01	2.56	0.83	2.92	0.76	1.04	1.88	2.08
1.19	1.79	2.81	2.46	1.88	1.24	1.56	1.57

P (0.92 < X < 1.54) = ?

3

1.60	2.49	1.73	2.47	0.85	1.53	2.56	2.35
2.64	1.38	3.81	2.00	1.01	3.54	2.45	1.23
1.98	1.10	2.19	1.64	2.24	2.36	3.09	1.56
2.59	1.97	1.37	3.68	1.55	2.04	2.20	3.41
2.95	2.57	2.37	2.40	1.06	2.09	0.70	2.73
0.45	1.84	3.30	1.97	1.26	1.67	2.41	1.79
2.99	2.38	2.90	1.35	2.34	2.60	1.91	2.46
2.28	2.96	2.43	2.74	2.06	2.76	2.39	2.92
0.42	2.04	2.59	0.86	2.95	0.79	1.07	1.91
2.11	1.22	1.82	2.84	2.49	1.91	1.27	1.59

P (0.91 < X < 1.55) = ?

4

1.62	1.63	2.52	1.76	2.50	0.88	1.56	2.59
2.38	2.67	1.14	3.84	2.03	1.04	3.57	2.48
1.86	2.01	1.13	2.22	1.67	2.27	2.38	3.12
1.59	2.62	2.00	1.40	3.71	1.58	2.07	2.23
3.44	2.98	2.60	2.40	2.43	1.09	2.12	0.73
2.76	0.18	1.87	3.32	2.00	1.29	1.70	2.44
1.82	3.02	2.41	2.93	1.38	2.37	2.63	1.94
2.49	2.31	2.99	2.46	2.77	2.09	2.79	2.42
2.95	0.45	2.07	2.62	0.89	2.98	0.82	1.10
1.94	2.14	1.25	1.83	2.87	2.52	1.94	1.30

P (0.90 < X < 1.56) = ?

5

3.31	1.15	1.43	2.27	2.47	1.58	2.18	3.20
2.85	2.27	1.63	1.95	1.96	2.85	2.09	2.83
1.21	1.89	2.92	2.71	3.00	1.74	4.17	2.36
1.37	3.90	2.81	1.59	2.34	1.46	2.55	2.00
2.60	2.78	3.45	1.92	2.95	2.33	1.73	4.04
1.91	2.40	2.56	3.77	3.31	2.93	2.73	2.76
1.42	2.45	1.06	3.09	0.31	2.20	3.66	2.33
1.62	2.03	2.77	2.15	3.35	2.74	3.26	1.71
2.70	2.96	2.27	2.82	2.64	3.32	2.79	3.10
2.42	3.12	2.75	3.28	0.78	2.40	2.95	1.22

P (0.89 < X < 1.57) = ?

6

2.46	1.70	2.44	0.82	1.50	2.53	2.32	2.61
1.35	3.78	1.97	0.98	3.51	2.42	1.20	1.95
1.07	2.16	1.61	2.21	2.33	3.06	1.53	2.56
1.94	1.34	3.63	1.52	2.01	2.17	3.38	2.92
2.54	2.34	2.37	1.03	2.06	0.67	2.70	1.12
3.24	1.91	1.20	1.61	2.35	1.73	2.93	2.32
2.84	1.29	2.28	2.54	1.85	2.40	2.22	2.90
2.37	2.68	2.00	2.70	2.33	2.86	0.36	1.98
2.53	0.80	2.89	0.73	1.01	1.85	2.05	1.16
1.76	2.78	2.43	1.85	1.21	1.53	1.54	2.43

P (1.08 < X < 1.68) = ?

7

1.67	2.41	0.79	1.41	2.50	2.29	2.58	1.32
3.75	1.94	0.95	3.48	2.39	1.17	1.92	1.04
2.13	1.58	2.18	2.30	3.03	1.50	2.53	1.91
1.31	3.62	1.49	1.98	2.14	3.35	2.89	2.51
2.31	2.34	1.00	2.03	0.64	2.67	0.09	1.78
1.81	3.27	1.94	1.23	1.64	2.38	1.76	2.96
2.35	2.87	1.32	2.31	2.57	1.88	2.43	1.88
2.93	2.40	2.71	2.03	2.76	2.36	2.89	0.39
2.01	2.56	0.83	2.92	0.76	1.04	1.88	2.08
1.19	1.79	2.81	2.46	1.88	1.24	1.56	1.57

P (1.07 < X < 1.69) = ?

8

1.62	1.63	2.52	1.76	2.50	0.88	1.56	2.59
2.38	2.67	1.14	3.84	2.03	1.04	3.57	2.48
1.86	2.01	1.13	2.22	1.67	2.27	2.38	3.12
1.59	2.62	2.00	1.40	3.71	1.58	2.07	2.23
3.44	2.98	2.60	2.40	2.43	1.09	2.12	0.73
0.45	1.84	3.30	1.97	1.26	1.67	2.41	1.79
2.99	2.38	2.90	1.35	2.34	2.60	1.91	2.46
2.28	2.96	2.43	2.74	2.06	2.76	2.39	2.92
0.42	2.04	2.59	0.86	2.95	0.79	1.07	1.91
2.11	1.22	1.82	2.84	2.49	1.91	1.27	1.59

P (1.06 < X < 1.70) = ?

9

1.60	2.49	1.73	2.47	0.85	1.53	2.56	2.35
2.64	1.38	3.81	2.00	1.01	3.54	2.45	1.23
1.98	1.10	2.19	1.64	2.24	2.36	3.09	1.56
2.59	1.97	1.37	3.68	1.55	2.04	2.20	3.41
2.95	2.57	2.37	2.40	1.06	2.09	0.70	2.73
2.76	0.18	1.87	3.32	2.00	1.29	1.70	2.44
1.82	3.02	2.41	2.93	1.38	2.37	2.63	1.94
2.49	2.31	2.99	2.46	2.77	2.09	2.79	2.42
2.95	0.45	2.07	2.62	0.89	2.98	0.82	1.10
1.94	2.14	1.25	1.83	2.87	2.52	1.94	1.30

P (1.05 < X < 1.71) = ?

10

1.43	2.03	3.05	2.70	2.13	1.48	1.80	1.81
2.70	1.94	3.63	1.06	1.74	2.77	2.56	2.85
1.59	3.08	2.21	1.22	3.75	2.66	1.44	3.19
1.81	2.40	1.85	2.45	2.57	3.30	1.77	2.80
3.18	1.58	2.89	1.76	2.25	2.41	3.62	2.13
1.95	0.45	2.07	2.62	0.89	2.98	0.82	1.10
1.94	2.14	1.25	1.83	2.87	2.52	1.94	1.30
1.62	1.03	2.77	2.15	2.35	2.74	3.26	1.71
2.70	2.96	2.27	1.82	2.64	3.32	2.79	3.10
2.42	1.12	2.75	1.28	0.78	2.40	2.95	1.22

P (1.04 < X < 1.72) = ?

11

2.46	1.70	1.43	2.27	2.47	1.58	2.32	2.61
1.35	3.78	1.63	1.95	1.96	2.85	1.20	1.95
1.07	2.16	1.87	3.32	2.00	1.29	1.53	2.56
1.94	1.34	2.41	2.93	1.38	2.37	3.38	2.92
2.54	2.34	2.99	2.46	2.77	2.09	2.70	1.12
3.24	1.91	2.07	2.62	0.89	2.98	2.93	2.32
2.84	1.29	1.25	1.83	2.87	2.52	2.22	2.90
2.37	2.68	2.77	2.15	3.35	2.74	0.36	1.98
2.53	0.80	2.27	2.82	2.64	3.32	2.05	1.16
1.76	2.78	2.75	3.28	0.78	2.40	1.54	2.43

$P(1.23 < X < 1.83) = ?$

12

3.31	1.15	2.44	0.82	1.50	2.53	2.18	3.20
2.85	2.27	1.97	0.98	3.51	2.42	2.09	2.83
2.76	0.18	1.61	2.21	2.33	3.06	1.70	2.44
1.82	3.02	3.63	1.52	2.01	2.17	2.63	1.94
2.49	2.31	2.37	1.03	2.06	0.67	2.79	2.42
2.95	0.45	1.20	1.61	2.35	1.73	0.82	1.10
1.94	2.14	2.28	2.54	1.85	2.40	1.94	1.30
1.62	2.03	2.00	2.70	2.33	2.86	3.26	1.71
2.70	2.96	2.89	0.73	1.01	1.85	2.79	3.10
2.42	3.12	2.43	1.85	1.21	1.53	2.95	1.22

$P(1.22 < X < 1.84) = ?$

13

1.60	2.49	0.79	1.41	2.50	2.29	2.56	2.35
2.64	1.38	0.95	3.48	2.39	1.17	2.45	1.23
1.98	1.10	2.18	2.30	3.03	1.50	3.09	1.56
2.59	1.97	1.49	1.98	2.14	3.35	2.20	3.41
2.95	2.57	1.00	2.03	0.64	2.67	0.70	2.73
2.76	0.18	1.94	1.23	1.64	2.38	1.70	2.44
1.82	3.02	1.32	2.31	2.57	1.88	2.63	1.94
2.49	2.31	2.71	2.03	2.76	2.36	2.79	2.42
2.95	0.45	0.83	2.92	0.76	1.04	0.82	1.10
1.94	2.14	2.81	2.46	1.88	1.24	1.94	1.30

$P(1.21 < X < 1.85) = ?$

14

0.67	2.41	1.73	2.47	0.85	1.53	1.58	1.32
0.75	1.94	3.81	2.00	1.01	3.54	1.92	1.04
2.13	1.58	2.19	1.64	2.24	2.36	2.53	1.91
1.31	3.62	1.37	3.68	1.55	2.04	2.89	2.51
2.31	0.34	2.37	2.40	1.06	2.09	0.09	1.78
1.81	2.27	1.87	3.32	2.00	1.29	1.76	2.96
2.35	2.87	2.41	2.93	1.38	2.37	2.43	1.88
2.93	2.40	2.99	2.46	1.77	2.09	2.89	0.39
2.01	2.56	2.07	2.62	0.89	2.98	1.88	2.08
1.19	1.79	1.25	1.83	2.87	2.52	1.56	1.57

$P(1.20 < X < 1.86) = ?$

15

1.62	1.63	2.52	1.76	2.50	0.88	1.56	2.59
2.38	2.67	3.14	3.84	2.03	1.04	3.57	2.48
2.86	2.01	3.13	2.22	1.67	2.27	2.38	3.12
1.59	2.62	2.00	1.40	3.71	1.58	2.07	2.23
0.42	2.04	2.59	0.86	2.95	0.79	1.07	1.91
2.11	3.22	1.82	2.84	2.49	2.91	3.27	1.59
1.76	2.50	1.88	3.08	2.47	2.99	1.44	2.43
2.69	2.00	2.55	2.37	3.05	2.52	1.83	2.15
2.85	3.48	3.01	0.51	2.13	2.68	0.95	3.04
0.88	1.16	2.00	3.20	1.31	1.91	2.93	2.58

$P(1.19 < X < 1.87) = ?$

9

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:

:

1)

, ;

2)

80%, 95% 99%

-

;

3)

;

4) , -
 (80%, 95%, 99%), -
 - ;

5) δ_γ ,

(80%, 95%, 99%): δ_{80} , δ_{95} , δ_{99} ;

6) ()
 (80%, 95%, 99%)

$$\left| \frac{\delta_\gamma}{y} \right| \cdot 100\% (\delta_\gamma \text{ y }) ;$$

7) , γ

1

:

		, %
1	1,24	39,4
2	0,63	23,2
3	1,18	37,2
4	1,12	35,1
5	0,44	20,0
6	1,19	37,9
7	0,48	20,1
8	0,65	23,4
9	0,26	13,4
10	0,75	24,8
11	1,03	32,2
12	0,89	30,2
13	0,16	10,3
14	0,67	23,7
15	0,90	31,3

2

:

	,	, %
1	38,9	10,7
2	33,3	11,3
3	37,7	12,2
4	31,1	12,4
5	29,4	10,9
6	37,2	11,3
7	35,6	11,1
8	34,1	14,0
9	0,26	6,8
10	22,8	7,1
11	21,7	8,9
12	26,	4,2
13	23,3	7,4
14	24,5	11,4
15	29,9	4,8

3

:

	,	, %
1	5,46	27,6
2	5,53	24,9
3	7,05	32,1
4	7,29	37,1
5	7,40	36,9
6	7,10	33,4
7	6,25	31,3
8	8,64	39,3
9	5,18	24,8
10	1,81	20,0
11	2,30	25,5
12	5,53	26,4
13	2,22	20,3
14	3,54	29,1
15	3,23	27,7

4

:

	,	, %
1	20,1	12,2
2	64,2	17,6
3	61,1	17,5
4	13,3	10,3
5	10,8	12,8
6	17,2	13,1
7	34,1	16,9
8	32,3	14,4
9	27,8	16,0
10	24,2	16,4
11	55,5	18,3
12	17,1	10,8
13	11,1	10,0
14	25,5	14,0
15	31,1	16,1

5

:

	,	, %
1	1,25	9,2
2	2,32	14,7
3	1,71	10,3
4	1,64	10,0
5	1,38	9,9
6	1,18	9,1
7	1,44	9,8
8	1,17	6,4
9	1,72	13,0
10	2,21	11,8
11	1,64	13,2
12	1,73	11,4
13	1,17	8,1
14	1,39	9,0
15	1,07	11,1

6

:

	,	, %
1	1,08	20,1
2	1,05	12,9
3	0,99	18,0
4	1,02	11,7
5	0,98	17,9
6	1,04	16,8
7	1,03	15,6
8	1,10	14,3
9	1,03	18,1
10	0,89	17,8
11	0,78	13,0
12	0,99	14,2
13	1,43	24,2
14	1,03	20,0
15	1,05	19,3

7

:

	,	, %
1	33,4	12,3
2	29,1	14,7
3	25,3	10,9
4	27,1	16,1
5	43,3	22,3
6	47,2	21,1
7	49,3	24,3
8	35,7	13,3
9	45,8	27,6
10	43,4	28,3
11	42,1	25,1
12	40,1	20,2
13	33,3	13,7
14	41,2	19,9
15	34,0	14,2

8

:

	, %	,
1	84	4300
2	83	4150
3	67	3000
4	63	3420
5	69	3300
6	70	4300
7	73	3420
8	81	4100
9	77	3700
10	72	3500
11	80	4000
12	85	4450
13	83	4270
14	70	3300
15	87	4500

9

:

	, %	%
1	18,1	9,5
2	7,8	19,4
3	7,4	8,7
4	6,4	18,3
5	7,8	16,4
6	17,1	8,8
7	10,2	17,8
8	14,1	13,7
9	20,0	7,0
10	16,7	10,2
11	16,0	10,4
12	20,4	7,3
13	16,2	10,7
14	16,0	14,0
15	20,1	7,3

:

	, %	,
1	40	142,20
2	33	152,33
3	37	154,20
4	39	149,95
5	37	154,37
6	41	149,80
7	49	170,11
8	38	168,33
9	55	193,30
10	43	172,72
11	56	189,39
12	47	187,01
13	44	173,40
14	55	187,87
15	54	184,20

:

	,	, %
1	20,0	2,0
2	12,8	1,8
3	9,2	1,1
4	5,3	3,5
5	18,6	10,1
6	10,8	3,3
7	28,7	24,2
8	13,8	1,9
9	28,6	20,8
10	22,9	19,2
11	14,0	3,4
12	13,0	2,7
13	12,8	1,4
14	25,0	20,1
15	13,8	7,8

:

	,	, %
1	80,0	20,0
2	87,2	37,5
3	90,8	43,4
4	94,7	45,6
5	81,4	23,4
6	89,2	25,0
7	71,3	17,2
8	86,2	33,3
9	71,4	15,0
10	77,7	18,7
11	86,0	24,8
12	87,0	34,5
13	87,2	33,1
14	75,0	19,2
15	86,2	31,8

:

	, %	%
1	25,2	9,5
2	58,2	9,4
3	42,2	8,7
4	46,8	8,3
5	60,5	6,4
6	66,1	8,8
7	26,5	7,8
8	59,9	13,7
9	43,2	7,0
10	47,8	6,7
11	61,8	10,4
12	68,1	7,3
13	32,0	8,9
14	60,2	9,4
15	44,2	7,3

:

	, %	, %
1	7,89	8,9
2	14,41	4,3
3	6,01	10,2
4	9,17	4,9
5	6,78	8,3
6	8,91	7,8
7	6,17	13,1
8	10,11	4,9
9	5,98	13,3
10	6,10	10,7
11	5,90	13,7
12	8,13	5,6
13	9,01	4,7
14	6,00	11,1
15	6,13	10,8

:

	, %	,
1	84	4300
2	83	4150
3	67	3000
4	63	3420
5	69	3300
6	70	4300
7	73	3420
8	81	4100
9	77	3700
10	72	3500
11	80	4000
12	85	4450
13	83	4270
14	70	3300
15	87	4500

- 1 . MathCad 2001: . - : , 2001. -
624 .
- 2 . . MathCad 2000. -
: . / . . , . . . - ∴ -
, 2000. - 656 .
- 3 . MathCad 2000: / . .
. ; . ∴ ; - ∴ , 2000. -
416 .
- 4 . /
. , . , . - 2- . , . - ∴ , 2001. - 575 .
- 5 . . -
. MathCad PRO: . . - ∴
. , 2003. - 431 .
- 6 . . MathCad 8. - ∴ , 2000. - 320 .

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MathCAD

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. . .6,75. .- .4,91.
190 . . 338.

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